

# Building explanation machines for Science

A Neuro-symbolic perspective

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Reasoning & Explainable AI (ExplAIIn) Lab



IPAM UCLA  
(January 2023)



MANCHESTER  
1824

The University of Manchester



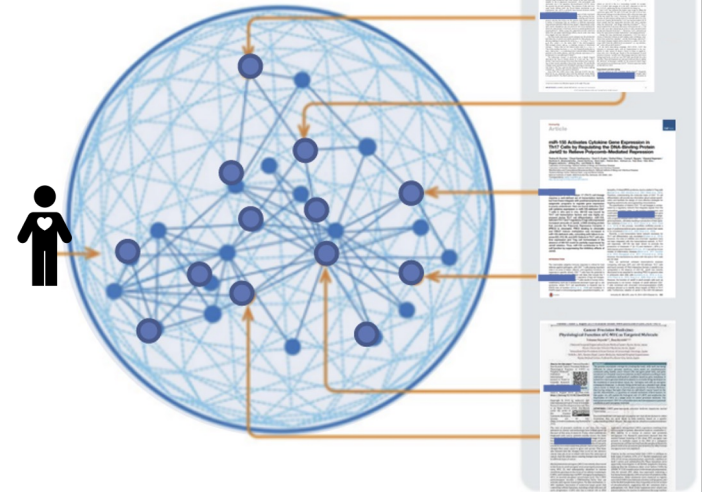
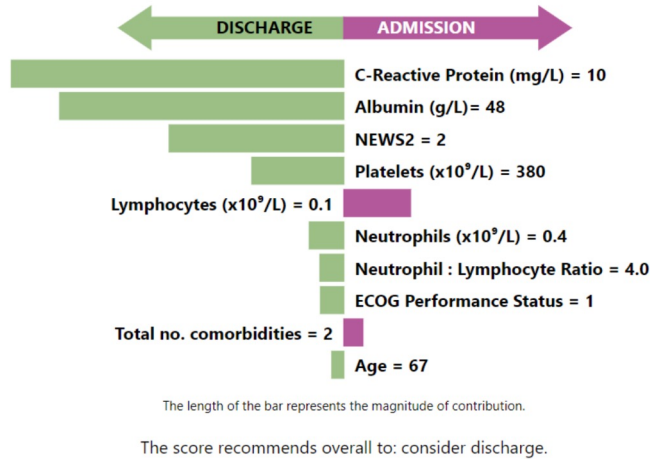


# ExplAIn Lab



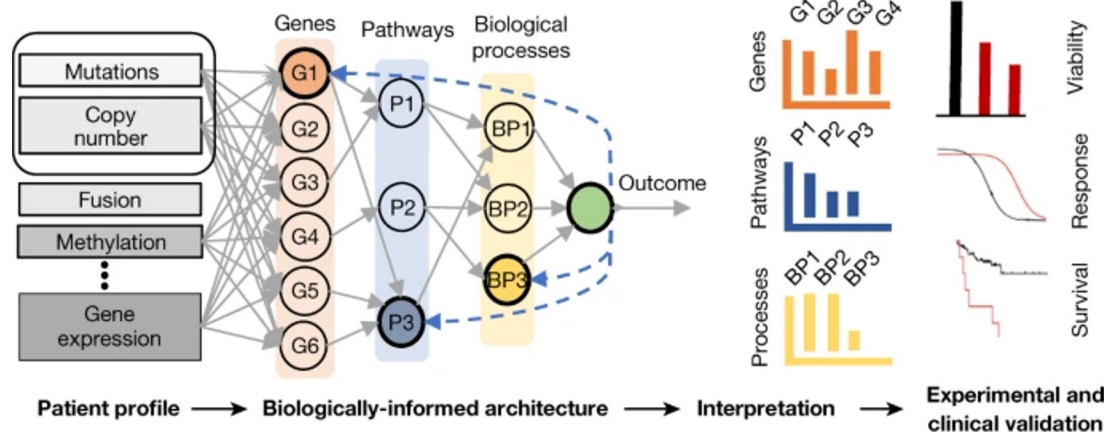
# Three Perspectives on Explanation

## Important Features Contributing to the Model Prediction for Your Patient



## Expert-AI Interaction

## Natural Language Explanations



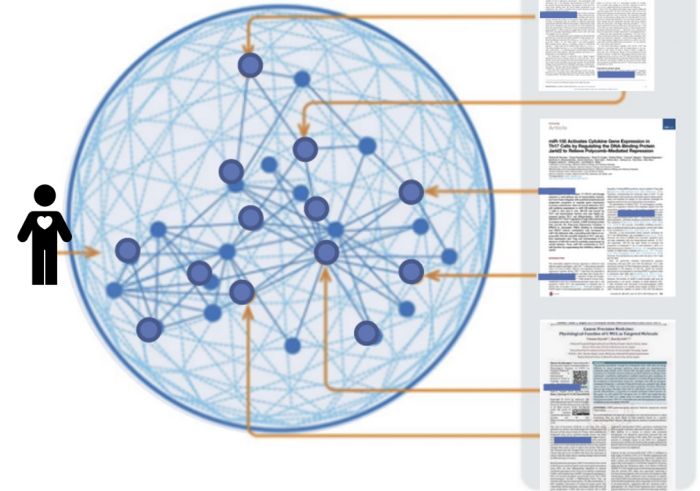
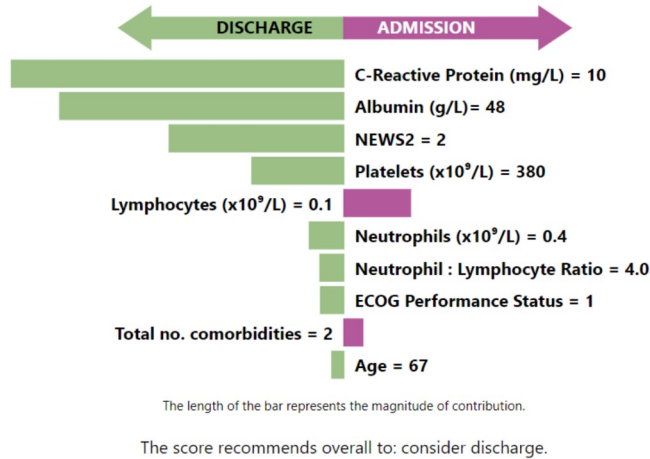
## Prior knowledge & explainability

Elmarakeby et al, Nature (2021)



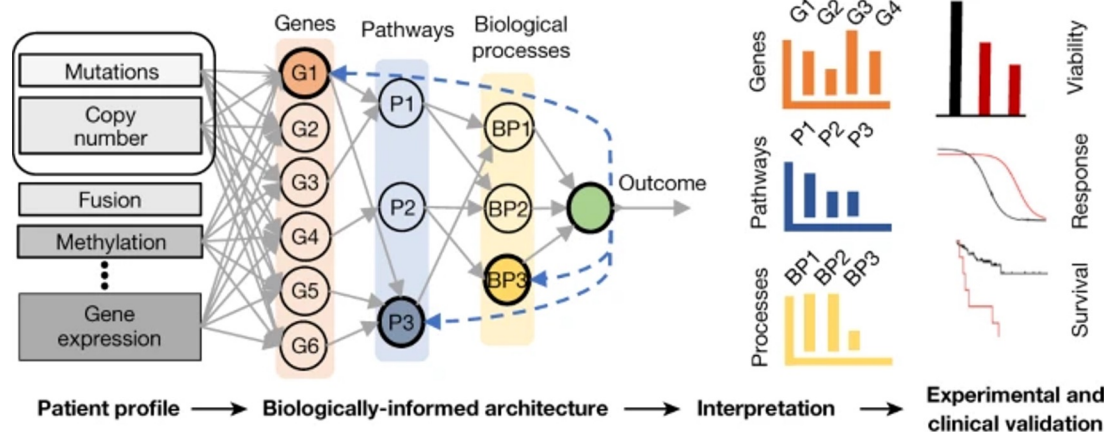
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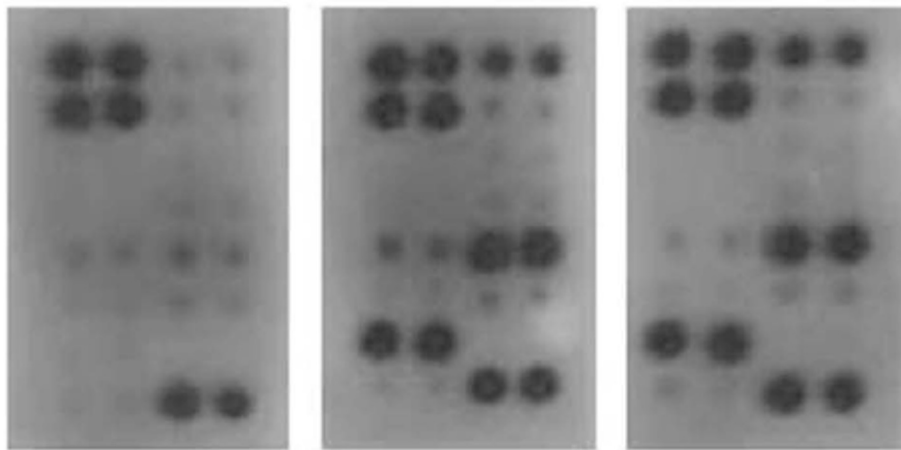


## Prior knowledge & explainability

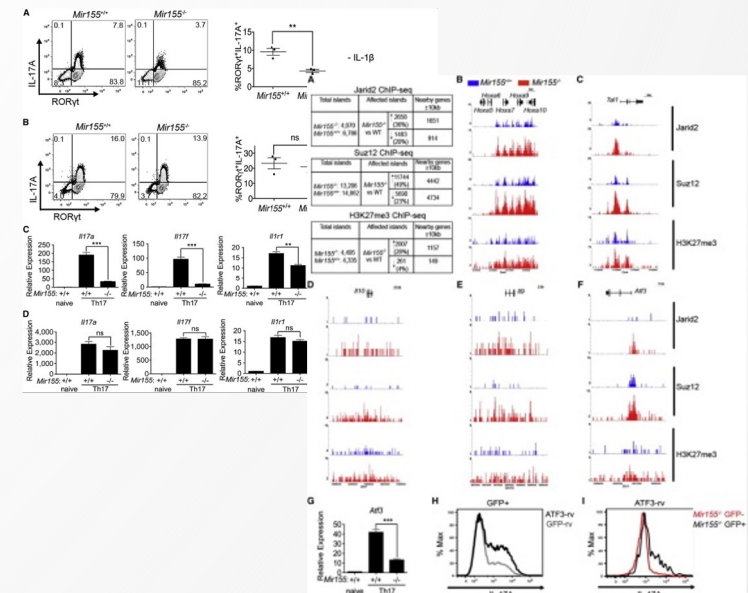
Elmarakeby et al, Nature (2021)

# Science, Inference & Language

## Experiment /Observations



## Analysis



## Conclusions

*miR-155 Activates Cytokine Gene Expression in Th17 Cells by Regulating the DNA-Binding Protein Jarid2 to Relieve Polycomb-Mediated Repression.*



**“miR-155 Activates Cytokine Gene  
Expression in Th17 Cells by Regulating the  
DNA-Binding Protein Jarid2 to Relieve  
Polycomb-Mediated Repression.”**

	<b>Patients with SARS-Cov-2 confirmed by PCR</b>	<b>Patients without SARS-Cov-2 confirmed by PCR</b>
<b>Median age (IQR)—years</b>	<b>63 (53–72)</b>	<b>60 (49–73)</b>
<b>Male</b>	<b>787/1,309 (60.1%)</b>	<b>90/167 (53.9%)</b>
<b>Race/ethnicity—Hispanic</b>	<b>577/1,268 (45.5%)</b>	<b>62/167 (37.1%)</b>
<b>Race/ethnicity—African American</b>	<b>278/1,268 (21.9%)</b>	<b>46/167 (27.5%)</b>
<b>Race/ethnicity—White</b>	<b>277/1,268 (21.8%)</b>	<b>43/167 (25.7%)</b>
<b>Race/ethnicity—Asian</b>	<b>73/1,268 (5.8%)</b>	<b>5/167 (3.0%)</b>
<b>Race/ethnicity—Other</b>	<b>63/1,268 (5.0%)</b>	<b>11/167 (6.6%)</b>
<b>Obesity (BMI ≥30)</b>	<b>465/1,176 (39.5%)</b>	<b>34/149 (22.8%)<sup>a</sup></b>
<b>Comorbidities—hypertension</b>	<b>420/1,268 (33.1%)</b>	<b>67/167 (40.1%)</b>
<b>Comorbidities—diabetes</b>	<b>293/1,268 (23.1%)</b>	<b>34/167 (20.4%)</b>
<b>Comorbidities—CKD</b>	<b>167/1,268 (13.2%)</b>	<b>27/167 (16.2%)</b>
<b>...</b>	<b>...</b>	<b>...</b>

**Del Valle et al. , *Nature Medicine* (2020)**



$$\frac{dx_1(t)}{dt} = x_2(t)$$

$$\frac{dx_2(t)}{dt} = ax_1(t) - bx_2(t)$$

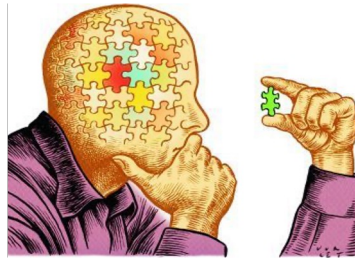
$$\frac{d^2x_1(t)}{dt^2} = \frac{dx_2(t)}{dt}$$

where  $x_1(t)$  is the serum concentration of cytokine  
and its rate of change by  $x_2(t)$

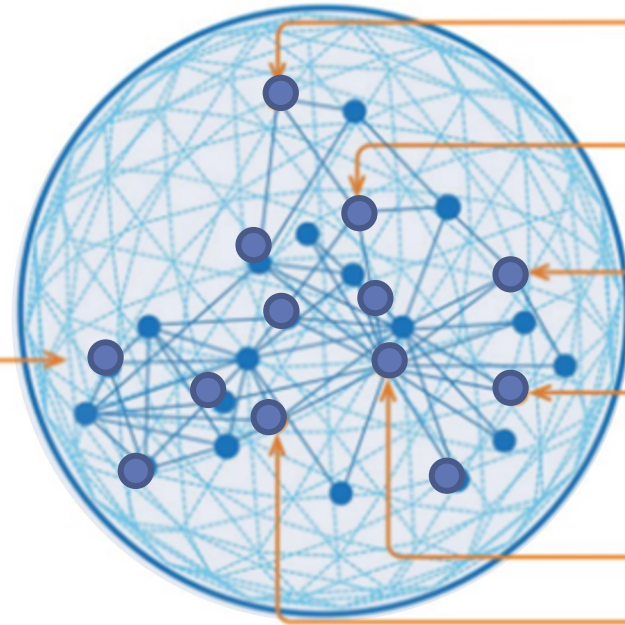
Language & Abstraction!

# What if we could infer over scientific facts at scale?

## Reassemble & repurpose



ANLI  
Models



Hypotheses  
Questions

Abductive Natural Language  
Inference (NLI)

Accumulated  
Knowledge

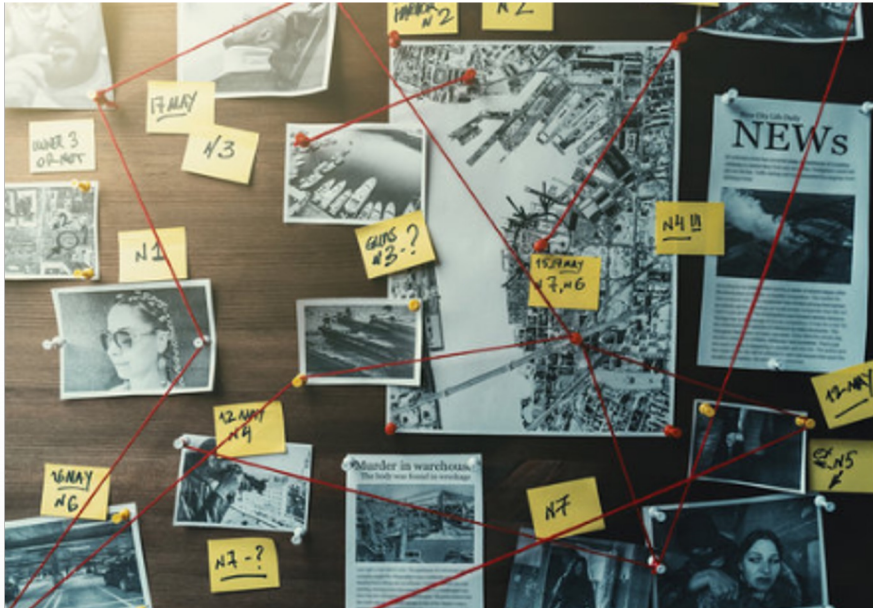
Adapted from: <https://human-centered.ai/project/explainable-ai-fwf-32554/>



# Abductive Reasoning

- First introduced by Peirce (1903).
- Inference to the best explanation.
- “Abduction is the mechanism via which we generate hypotheses about what we observe.”
- Dialogues closely with assumed background knowledge.

Veen, Creative leaps in theory: the might of abduction (2021)



# Abductive Natural Language Inference (ANLI)

Inference to the best explanation  
(facts, evidence)

**Claim:** Specialized cells protect the human body from disease-causing microbes by producing chemicals that destroy the microbes.

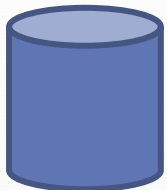
**True | False**

Why? (Explanation)

Multi-hop  
Multi-premise

Specialized cells are a source of chemicals that destroy disease-causing microbes.

disease-causing microbes have a negative impact on the body.



~10.000 facts



# Abductive Natural Language Inference (ANLI)

Inference to the best explanation  
(facts, evidence)

**Claim:** Specialized cells protect the human body from disease-causing microbes by producing chemicals that destroy the microbes.

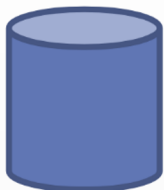
**True | False**

**Why? (Explanation)**

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~10.000 facts

Encoding scientific statements

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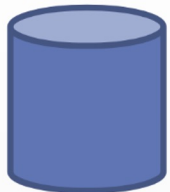
Multi-hop  
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Encoding inference relations

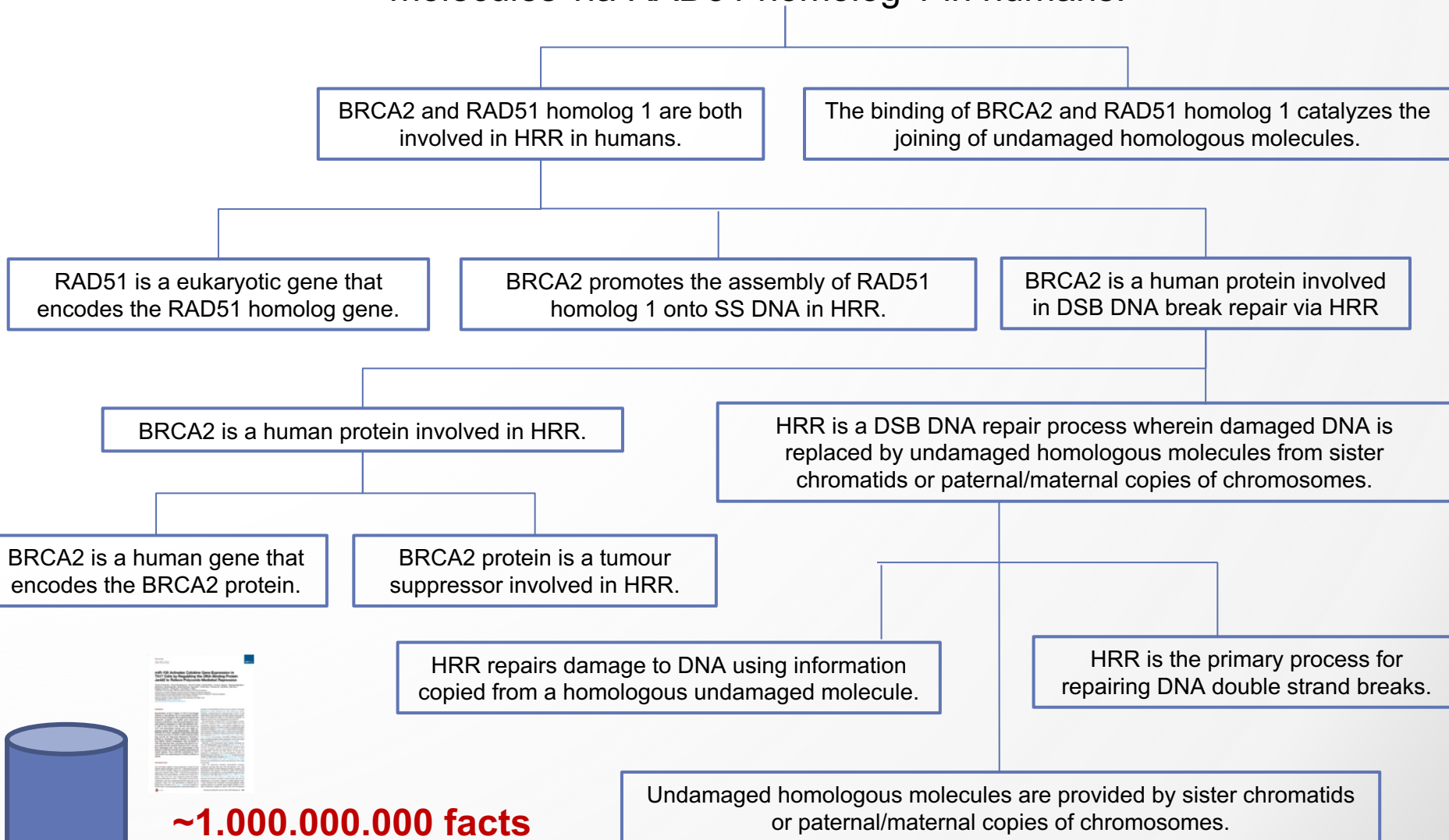
~10.000 facts



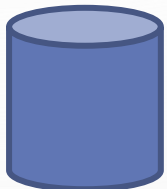


# Expert-level scientific inference & explanation

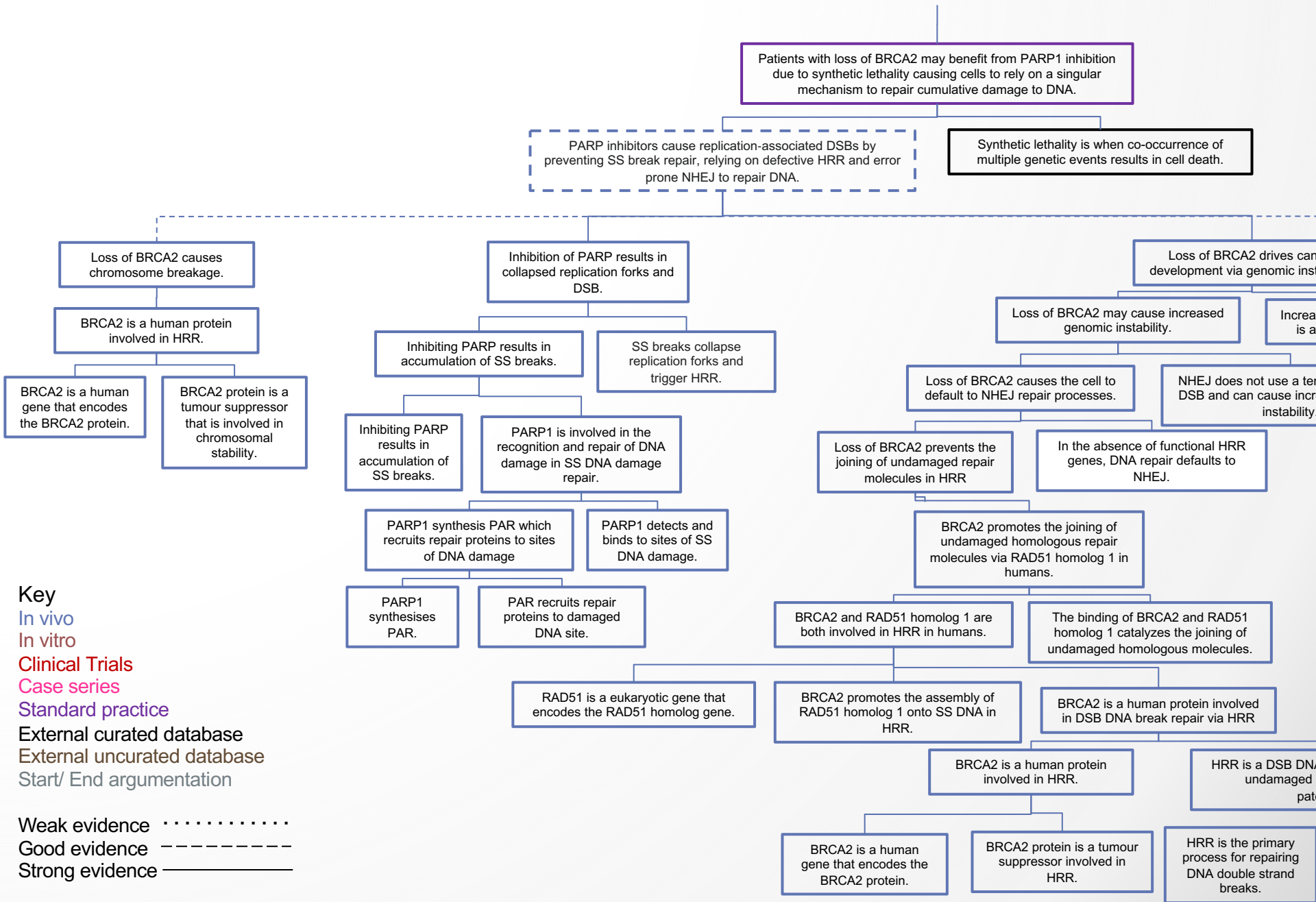
**Claim:** BRCA2 promotes the joining of undamaged homologous repair molecules via RAD51 homolog 1 in humans.



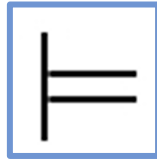
**~1.000.000.000 facts**



# Prostate cancer patient with loss of BRCA2 may benefit from PARP1 inhibition



Patients living in the San Francisco area with ErbB2+ breast cancer, a body weight > 60 kg, and a history of treatment with Cyclophosphamide in the last year, are eligible for this clinical trial.



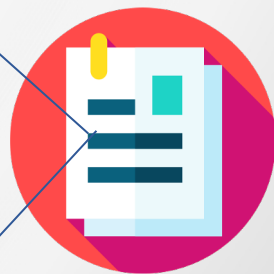
## Clinical Trial Report - Eligibility Criteria

### Inclusion criteria

- Patients with a history of chemotherapy treatment within the last 24 months.
- Age  $\geq$  60 years
- HER2-positive T1 histologically confirmed invasive carcinoma of the breast.
- Body weight > 110 lbs
- Patients be California residents

### Exclusion criteria

- Pregnant women





# The Neural Perspective: Language Models

- Probability distributions over strings of text.

The students opened their ...

The students opened their books  
(predicted)

**S** = The students opened their books

**P(S)** =  $P(\text{The}) \times P(\text{students} \mid \text{The}) \times P(\text{opened} \mid \text{The students}) \times P(\text{their} \mid \text{The students opened}) \times P(\text{books} \mid \text{The students opened their})$

# Neural Language Models

output distribution

$$\hat{y} = \text{softmax}(\mathbf{U}\mathbf{h} + \mathbf{b}_2) \in \mathbb{R}^{|V|}$$

hidden layer

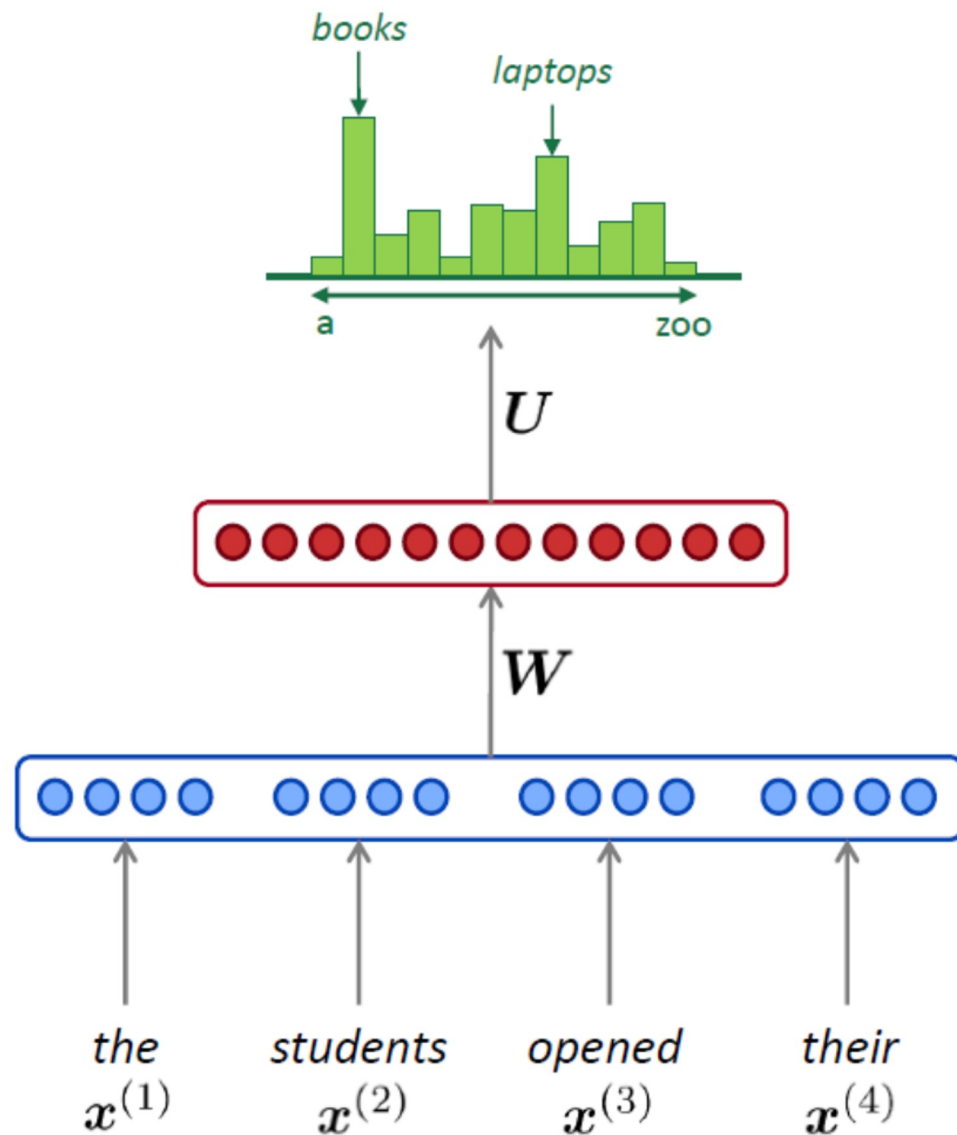
$$\mathbf{h} = f(\mathbf{W}\mathbf{e} + \mathbf{b}_1)$$

concatenated word embeddings

$$\mathbf{e} = [\mathbf{e}^{(1)}; \mathbf{e}^{(2)}; \mathbf{e}^{(3)}; \mathbf{e}^{(4)}]$$

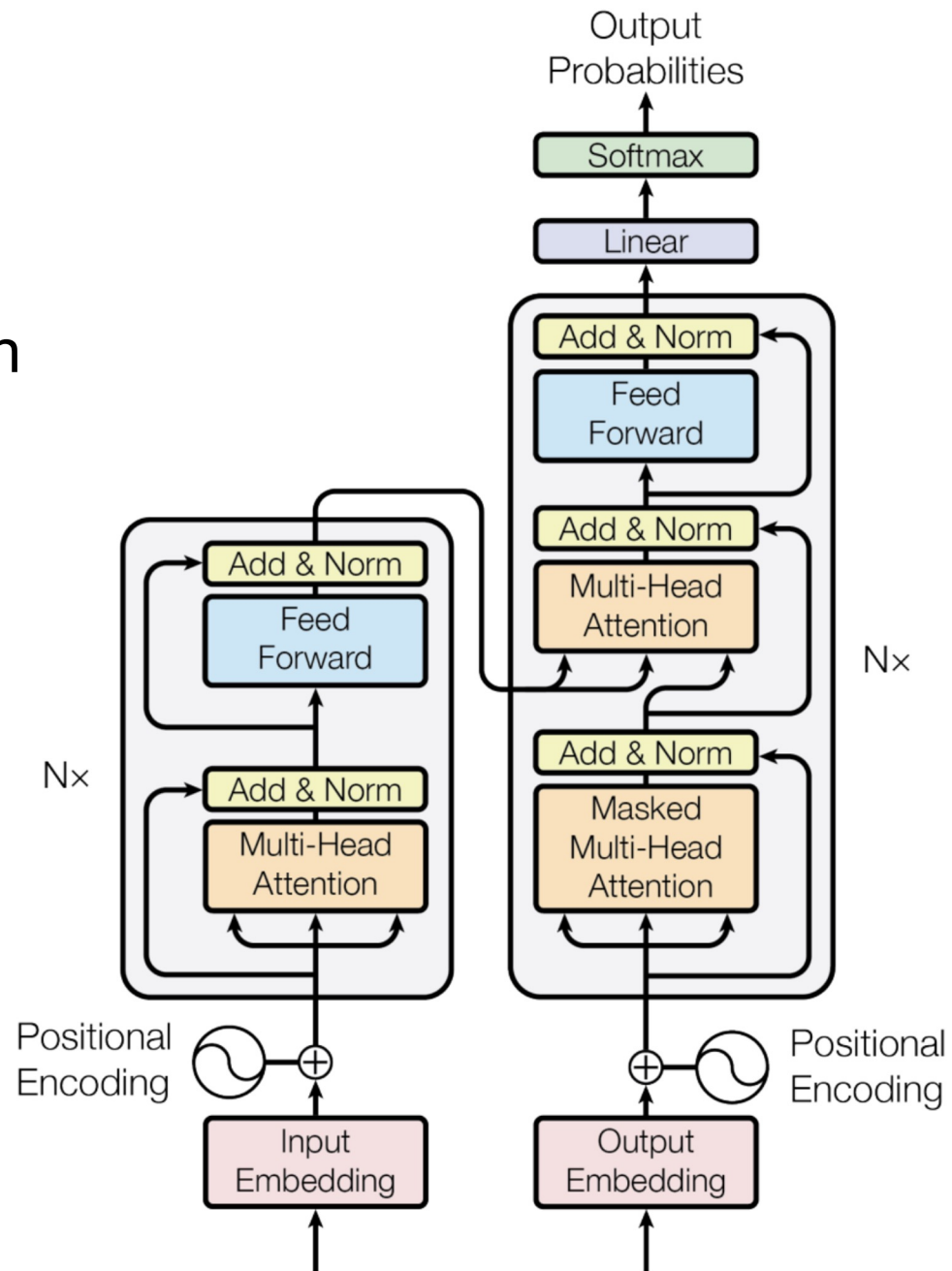
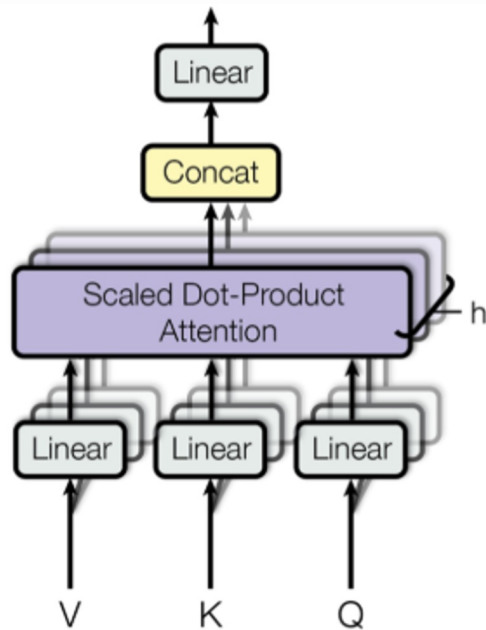
words / one-hot vectors

$$\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \mathbf{x}^{(3)}, \mathbf{x}^{(4)}$$



# Transformers

1. Positional Encodings
2. (Multi-head) Self-Attention

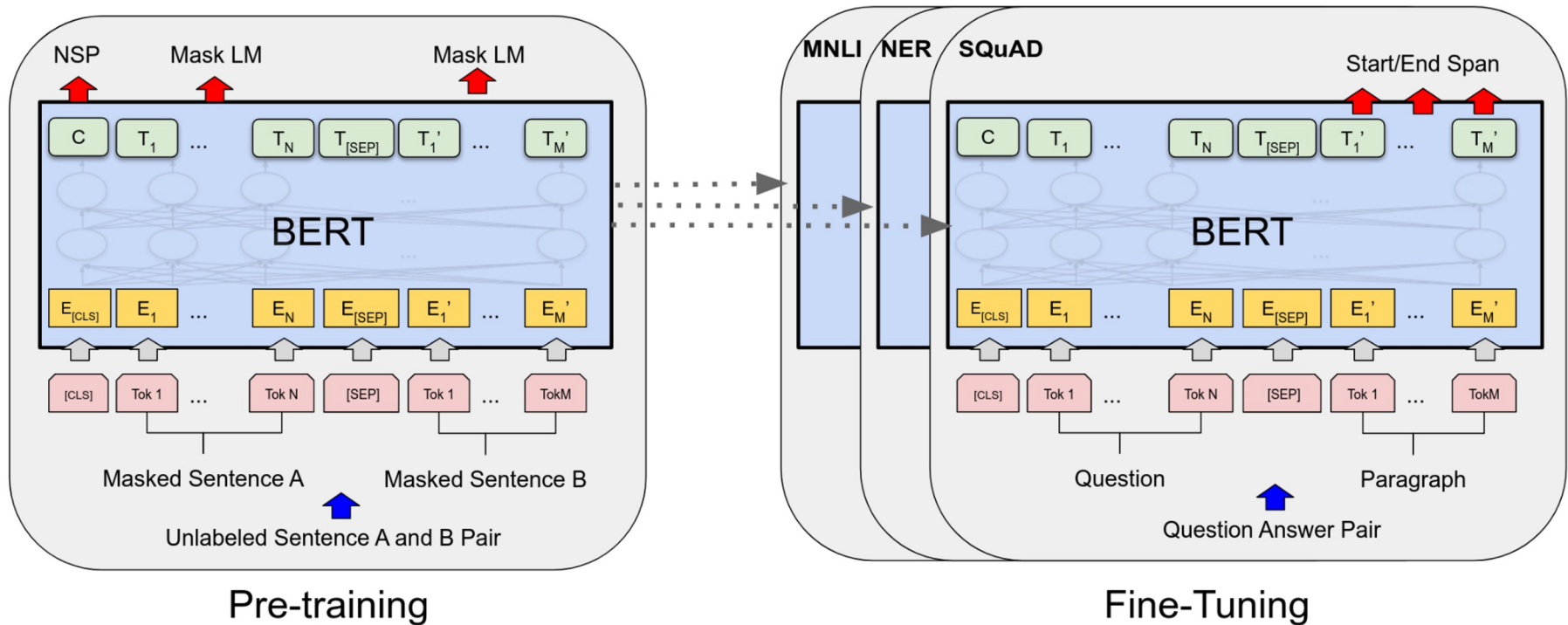




# BERT: Bidirectional Encoder Representations

## from Transformers

Self-attention allows a model to assign a meaning to a term in a complex context.



# Trust me, I am a Language Model.

Here is a sequence for a protein:

[START\_AMINO]MEEPQSDPSVEPPLSQETFSDLWKLLPE... [END\_AMINO]

And here is an isomeric SMILES for a compound:

[START\_I\_SMILES]CC(O)(P(=O)(O)O)P(=O)(O)O[END\_I\_SMILES]

**Question:** Will the the chemical compound be active against this protein?

**Answer:** No

# Trust me, I am a Language Model.

## Prompt

The formula for Bessel's differential equation is:

## Generated Answer

$$x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + (x^2 - \alpha^2) y = 0$$

## Prompt

Sulfuric acid reacts with sodium chloride, and gives \_\_\_\_\_ and \_\_\_\_\_:

`\[ \ce{ NaCl + H2SO4 ->`

## Generated Answer





# Why Meta's latest large language model survived only three days online

Galactica was supposed to help scientists. Instead, it mindlessly spat out biased and incorrect nonsense.

By Will Douglas Heaven

November 18, 2022



**Michael Black**

@Michael\_J\_Black · [Follow](#)



I asked [#Galactica](#) about some things I know about and I'm troubled. In all cases, it was wrong or biased but sounded right and authoritative. I think it's dangerous. Here are a few of my experiments and my analysis of my concerns. (1/9)

7:47 AM · Nov 17, 2022

Ouch!



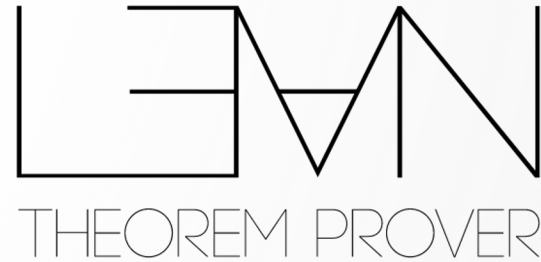
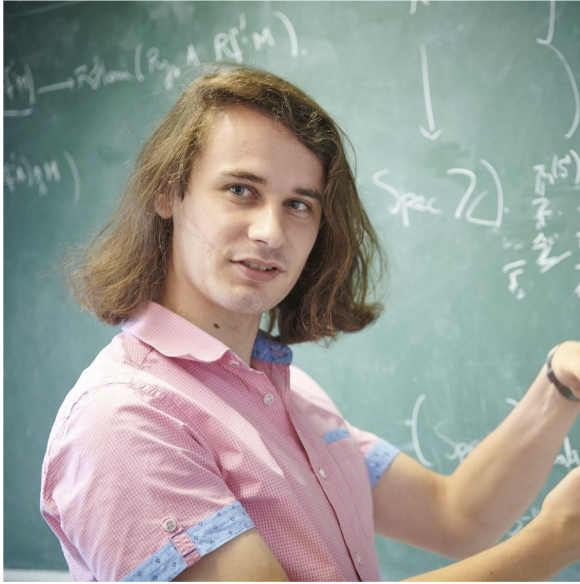
**Julian Togelius**

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My considered opinion of Galactica: it's fun, impressive, and interesting in many ways. Great achievement. It's just unfortunate that it's being touted as a practical research tool, and even more unfortunate that it suggests you use it to write complete articles.

# The Liquid Tensor Experiment



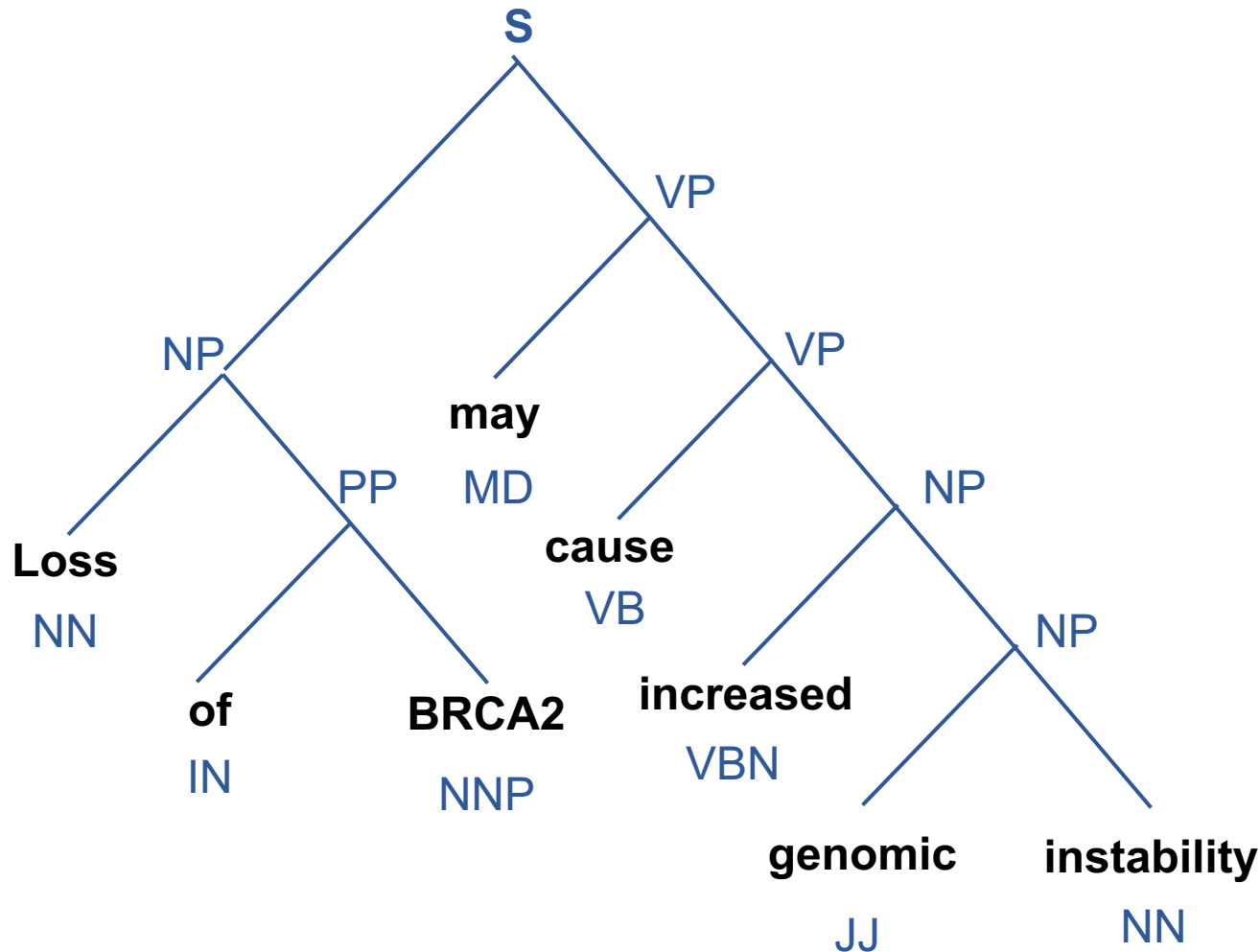
Why do I want a formalization?

— “with this theorem, the hope that the condensed formalism can be fruitfully applied to real functional analysis stands or falls. I think the theorem is of utmost foundational importance, **so being 99.9% sure is not enough.**”

Verifiability

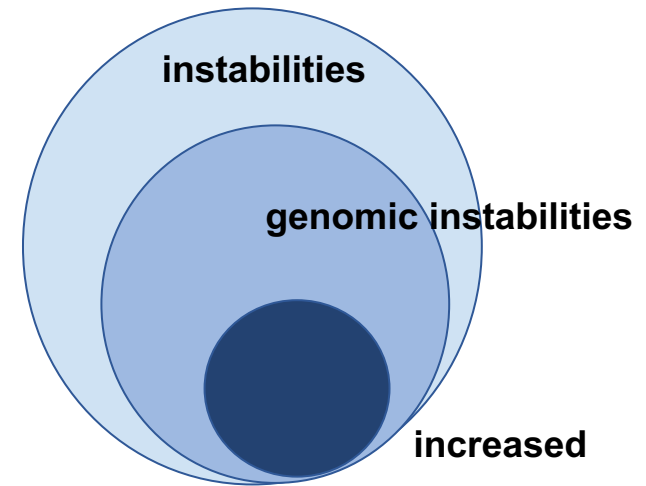
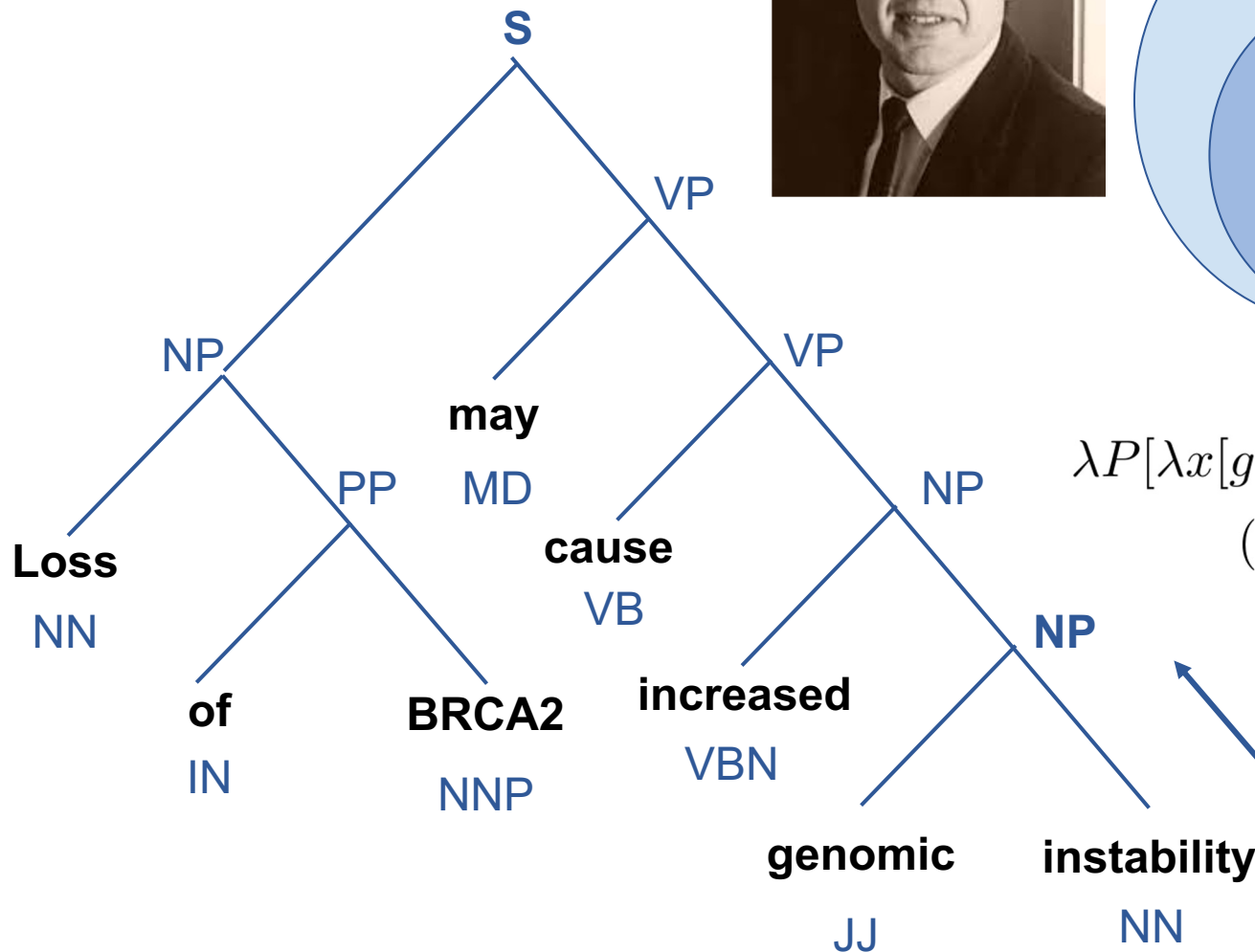
# The Formal Perspective

Loss of BRCA2 may cause increased genomic instability.





# The Formal Perspective



$$\lambda P[\lambda x[\text{genomic}(x) \wedge P(x)]]$$

$$(\lambda y[\text{instability}(y)])$$

# Scientific inference

## Scientific discourse

- Step-wise explicit (verbalised) inference.
- Formal, verifiable argument & explanation.
- Preserving the positive aspects of LLMs.
- Improving control.

Large Language  
Models (LLMs)

Formal



Neuro

Neuro-symbolic

Symbolic



# Scientific inference

## Scientific discourse

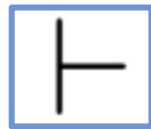
- Step-wise explicit (verbalised) inference.
- Formal, verifiable argument & explanation.
- Preserving the positive aspects of LLMs.
- Improving control.

$$\Gamma \models \Phi$$

$\Gamma$  semantically entails  $\Phi$

$$\Gamma \vdash \Phi$$

$\Gamma$  proves  $\Phi$



- interpretability

- control (inference guarantees)

# Encoding scientific statements



# Semantic Role Labeling

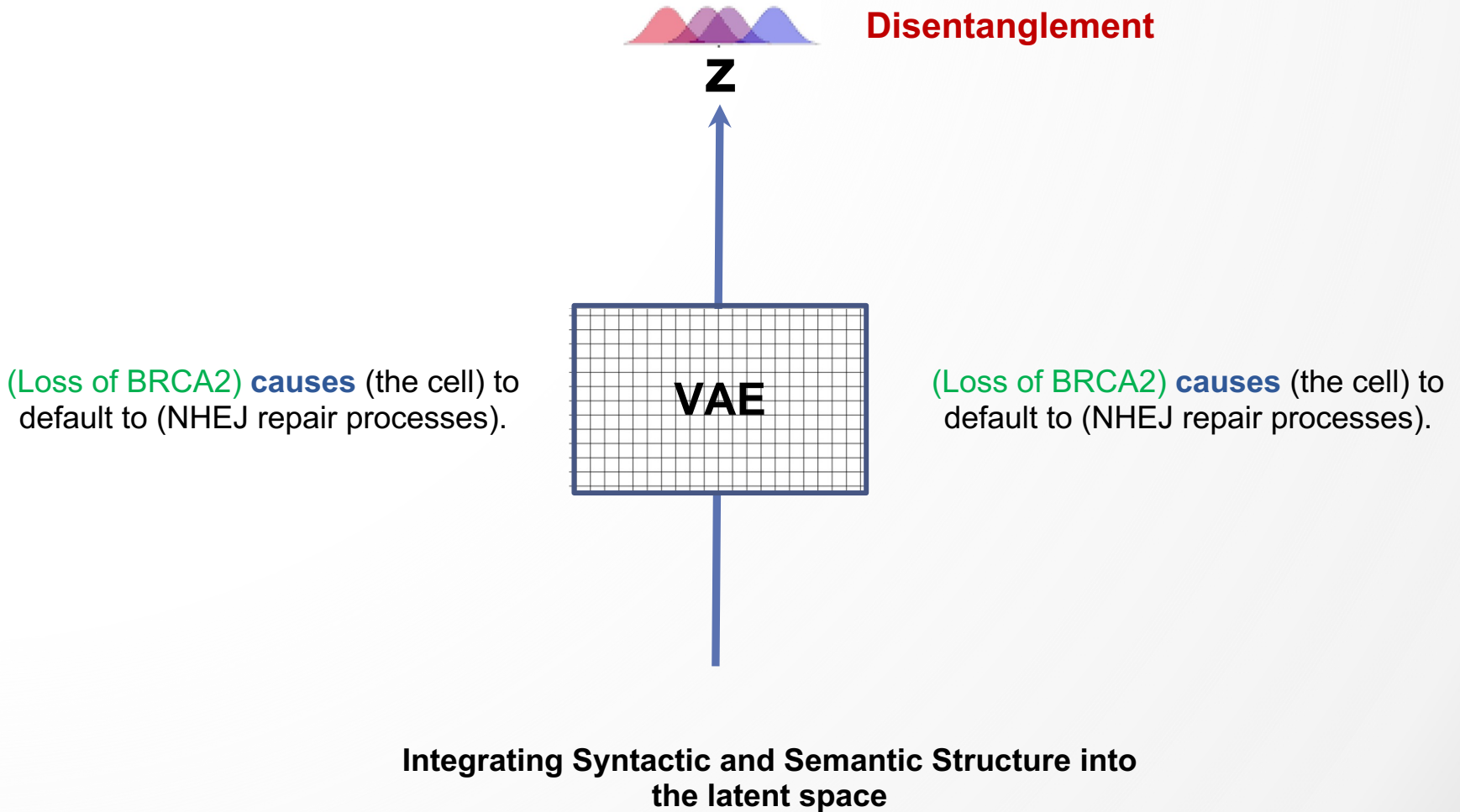


Animals	require	food	for survival	.
ARG0	V	ARG1	ARGM-PRP	

- Lightweight representation (a little semantics goes a long way).
- Robust parsers.
- Expressive semantic roles.

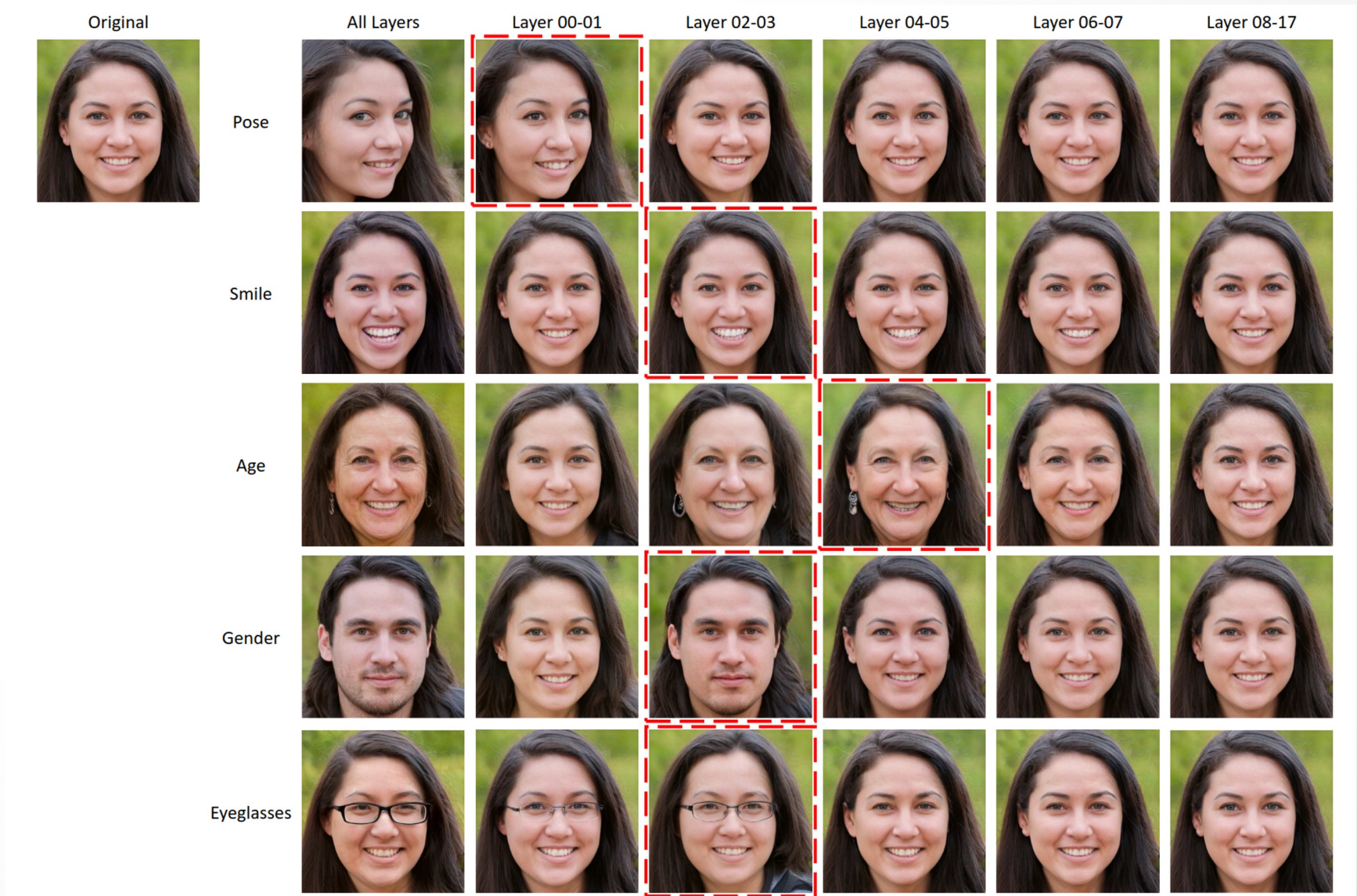
ARGM-DIR	Directionals. E.g. all waves transmit energy <b>from one place to another</b>
ARGM-PNC	Purpose. E.g. many animals blend in with their environment <b>to not be seen by predators</b>
ARGM-CAU	Cause. E.g. cold environments sometimes are white in color <b>from being covered in snow</b>
ARGM-PRP	Purpose. E.g. a pot is made of metal <b>for cooking</b>
ARGM-EXT	Extent. E.g. as the amount of oxygen exposed to a fire increases the fire will burn <b>longer</b>
ARGM-LOC	Location. E.g. a solute can be dissolved <b>in a solvent</b> when they are combined
ARGM-MNR	Manner. E.g. fast means <b>quickly</b>
ARGM-MOD	Modal verbs. E.g. atom <b>can</b> not be divided into smaller substances
ARGM-DIS	Discourse. E.g. if something required by an organism is depleted <b>then</b> that organism must replenish that something
ARGM-GOL	Goal. E.g. We flew <b>to Chicago</b>
ARGM-NEG	Negation. E.g. cactus wrens building nests in cholla cacti does <b>not</b> harm the cholla cacti
ARGM-ADV	Adverbials
ARGM-PRD	Markers of secondary predication. E.g.
ARGM-TMP	Temporals. E.g. a predator <b>usually</b> kills its prey to eat it
O	Empty tag.
V	Verb.
ARG0	Agent or Causer. E.g. <b>rabbits</b> eat plants
ARG1	Patient or Theme. E.g. rabbits eat <b>plants</b>
ARG2	indirect object / beneficiary / instrument / attribute / end state. E.g. animals are <b>organisms</b>
ARG3	start point / beneficiary / instrument / attribute. E.g. sleeping bags are designed <b>to keep people warm</b>
ARG4	end point. E.g. when water falls from the sky that

# Generative Models





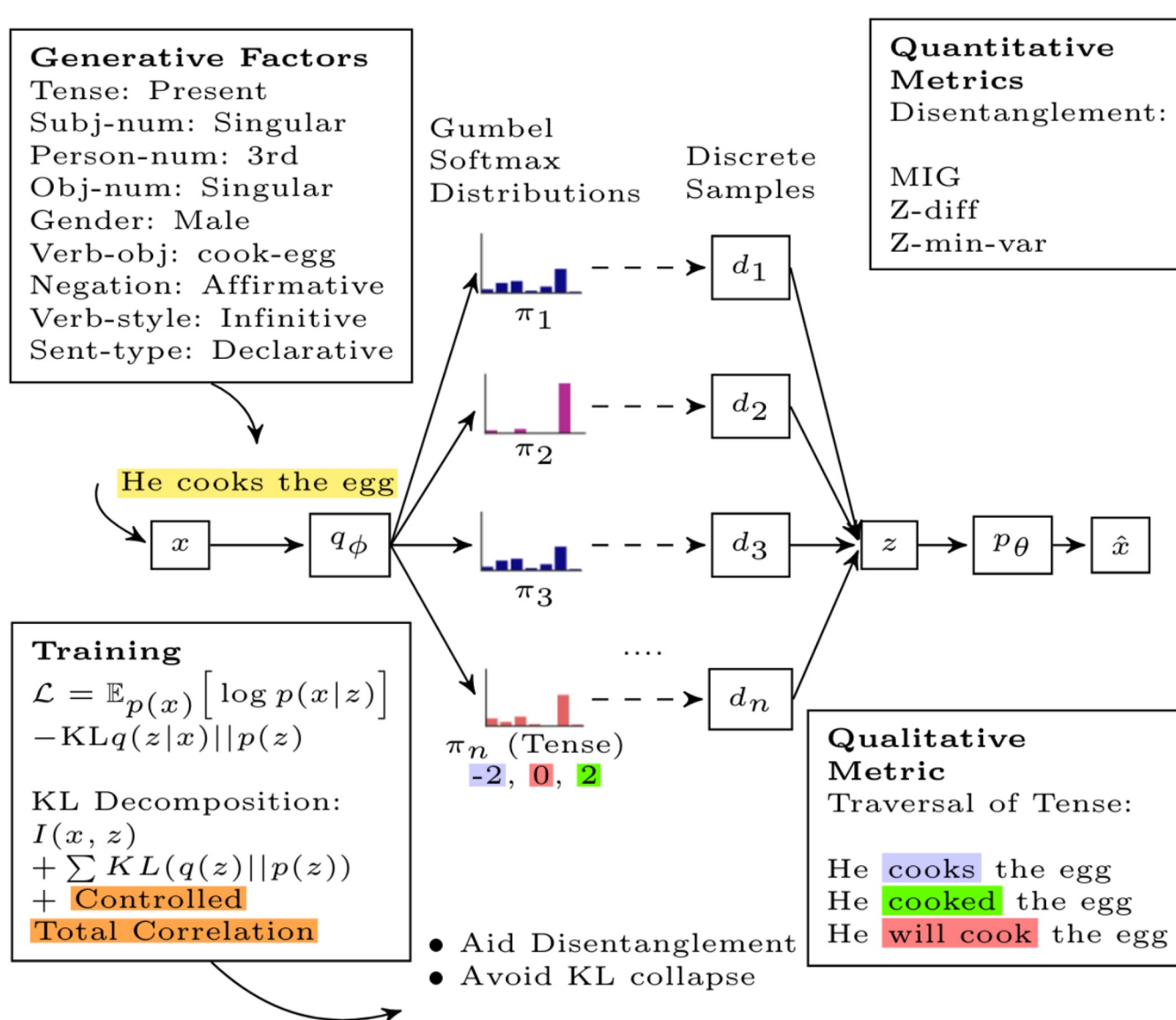
# Generative Models



*InterFaceGAN: Interpreting the Disentangled Face Representation Learned by GANs*



# Syntactic Disentanglement



# Syntactic Disentanglement

(Loss of BRCA2) **causes** (the cell) to default to (NHEJ repair processes).

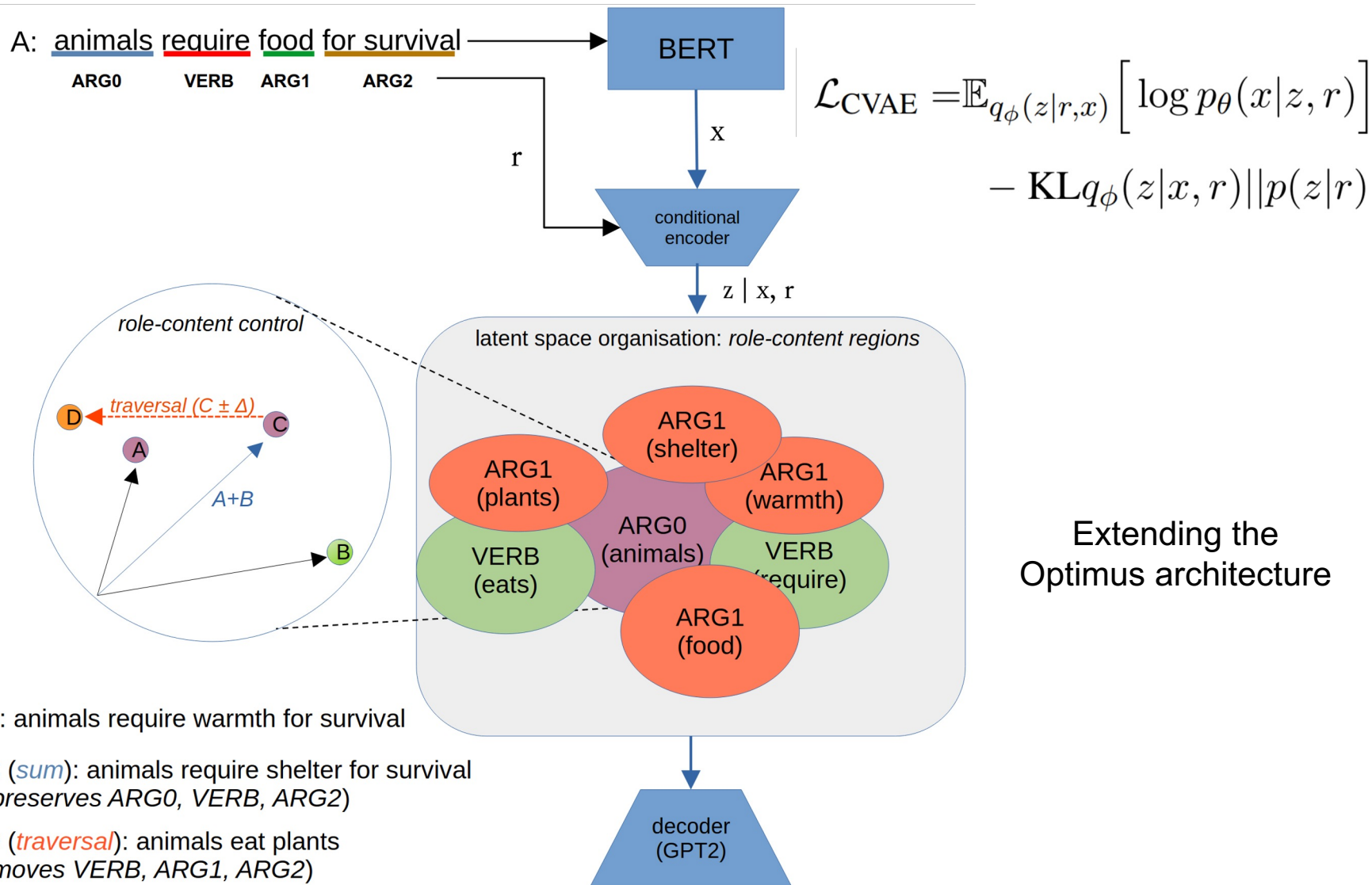
(Loss of BRCA2) **caused** (the cell) to default to (NHEJ repair processes).

(Loss of BRCA2) **does not cause** (the cell) to default to (NHEJ repair processes).

	Tense	Subject-number
input	you <b>will</b> not attend the party	<b>we</b> will not attend the party
$\beta$ VAE	you <b>will</b> not attend the party you <b>will</b> not <b>sign the paper</b> you <b>will</b> not attend the party	we will not attend the party <b>he</b> will not attend the party
JointVAE	you <b>will</b> not attend the party you <b>did</b> not <b>join the wedding</b> you <b>do</b> not attend the party	we will not attend the party <b>you</b> will not attend the party
DCTC	you <b>will</b> not attend the party you <b>did</b> not attend the party you <b>do</b> not attend the party	we will not attend the party <b>i</b> will not attend the party

## Latent traversal

# Syntactic-Semantic Disentanglement



# Syntactic-Semantic Disentanglement

an automobile is a kind of vehicle

an automobile requires a driver to move it  
an automobile is a kind of object

an airplane is a kind of vehicle  
a car is a kind of vehicle

an airplane is used for carrying passengers  
an airplane is a kind of object

**Latent traversal**

animals require food for survival

animals require warmth for survival

animals eat plants

animals produce milk

animals usually eat plants

animals eat berries ; plants

animals require food to survive

animals require shelter to survive

animals adapt to changing environments

animals obtain spices for cooking

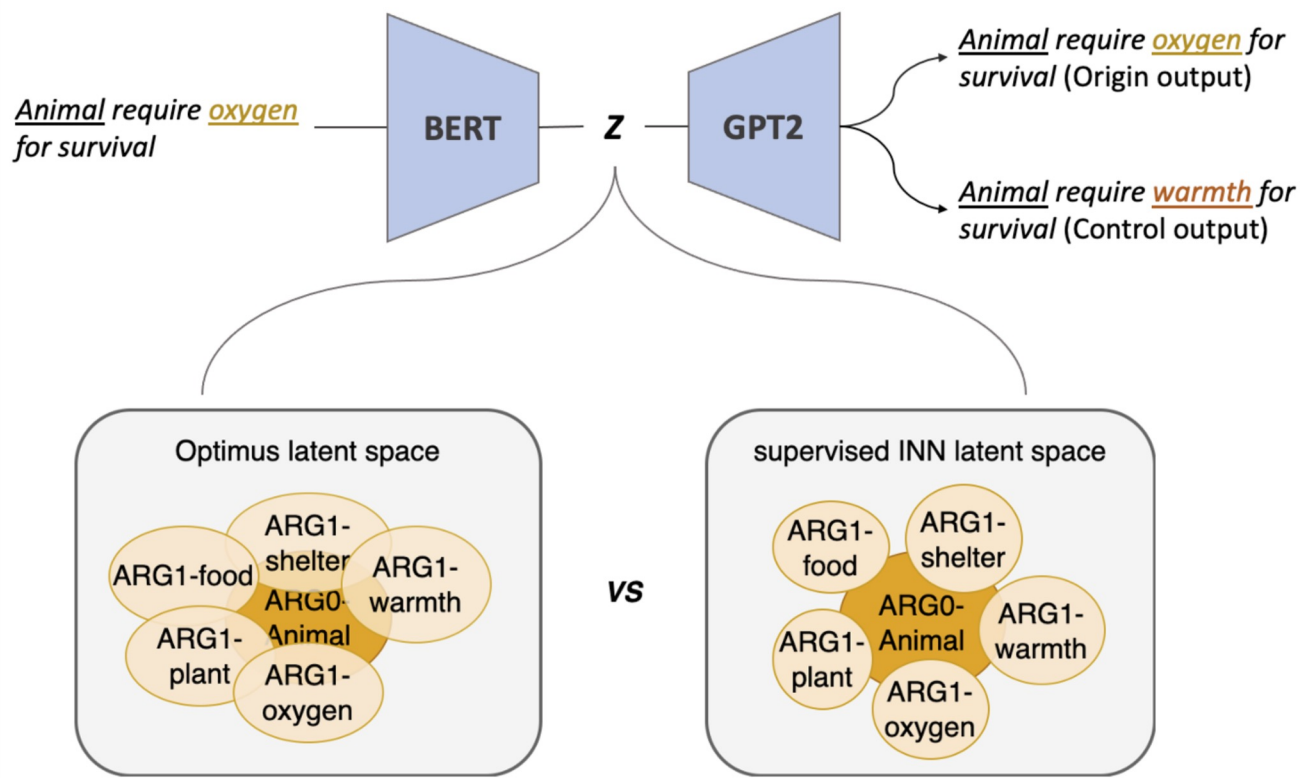
**Vector arithmetic  
(addition)**



# Improving Separability

Adding a flow-based INN component to improve separability

$$\mathcal{L}_{\text{sup}} = -\mathbb{E}_{x \sim p_{\text{cluster}}(x)} \frac{\left[ T(E(x)) - \mu_{\text{cluster}} \right]^2}{1 - \sigma^2} - \log |T'(E(x))|$$



## Interpolation

humans eat seeds

1. humans eat fruits
  2. humans eat seeds
  3. humans eat insects
  4. humans eat meat
  5. humans eat plants
  6. some animals eat prey
  7. some animals must eat to survive
  8. some animals must hunt for food
  9. some animals must hunt their prey to survive
- some animals must hunt to survive

## Interpolation

## Latent traversal

Input: some animals must hunt to survive

dim01: some animals must hunt for food  
dim01: some animals must hunt prey to survive  
dim01: some animals need to hunt to survive

dim12: an animal needs to breathe to survive  
dim12: an animal can fly without air  
dim12: a predator must hunt to survive

## Data Augmentation

Role-content	Augmented sentences
ARG0-animal	<p>an animal requires energy to move animals produce offspring some adult animals lay eggs an animal requires shelter an animal can use its body to breathe</p>
ARG0-human	<p>humans travel sometimes humans usually use gasoline humans sometimes endanger themselves humans use coal to make food humans depend on pollinators for survival</p>
PRED-are	<p>wheels are a part of a car lenses are a part of eyeglasses toxic chemicals are poisonous green plants are a source of food for animals copper and zinc are two metals</p>
PRED-mean	<p>summit mean the top of the mountain colder mean a decrease in heat energy helping mean something can be done better cleaner mean ( less ; lower ) in pollutants friction mean the product of a physical change</p>

# Representing concepts and definitions

- Essential attributes of a conceptualisation.
- Abundance of NL definitions in scientific discourse.
- Definition RL: Decomposing conceptual components.

DEFINIENDUM DIFFERENTIA QUALITY SUPERTYPE DIFFERENTIA-EVENT

**Homologous recombination repair** is a **DNA repair process** that includes the invasion of an undamaged DNA molecule by a damaged molecule of identical or very similar sequence.



DSR Optimus

a migratory aquatic bird found in the temperate regions  
of the northern hemisphere

1 a migratory bird of the eastern Mediterranean

2 a marine gastropod of the subfamily

3 a terrestrial aquatic mammal of the family

4 a terrestrial aquatic mammal of the suborder

5 a terrestrial invertebrate

6 a microscopic organism or invertebrate

a microscopic terrestrial animal or protozoan

an automobile

1 a motorcycle

a bicycle

## Interpolation

ADD

a flying machine

a flying creature

a flying dinosaur

a flying robot

a flying object

AVG

to make four copies of

to make five copies of

to make one copy of

to make two copies of

to make 3 copies of

## Latent traversal

SUB

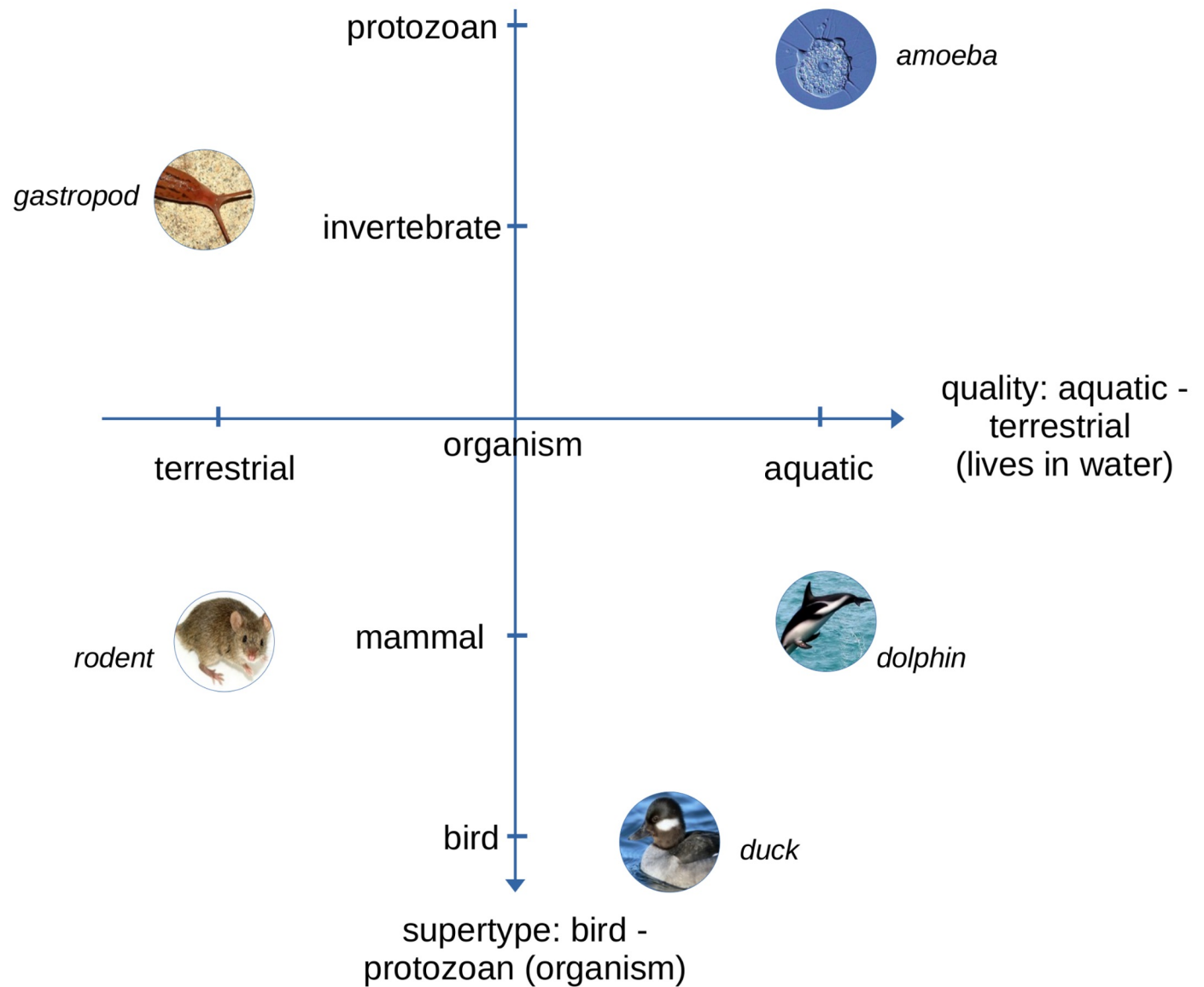
a female monarch

a monarch

the subnormal condition in females originating from...

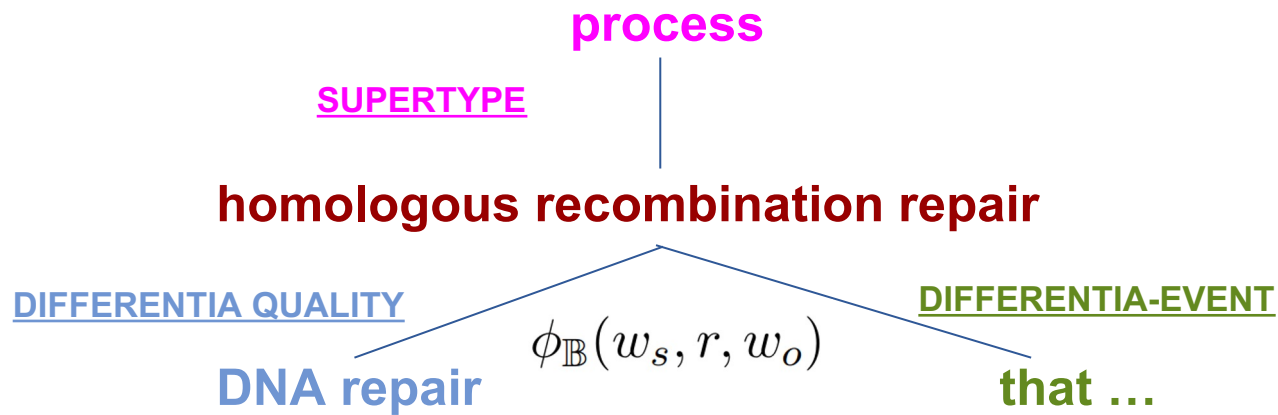
the normal female pregnancy associated with some

the female given name in the Japanese game...



# Multi-relational Hyperbolic Embeddings

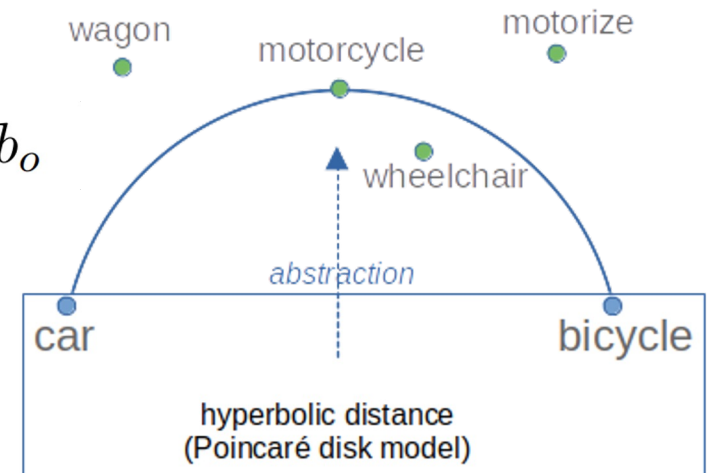
Induction of a hierarchical, multi-relational, multi-resolution conceptual representation. Abstracts OOV words.



Learn as a link prediction problem via a translational objective function in hyperbolic space.

$$\phi_{\mathbb{B}}(w_s, r, w_o) = -d_{\mathbb{B}}(\mathbf{h}_s^{(r)}, \mathbf{h}_o^{(r)})^2 + b_s + b_o$$

$$d_{\mathbb{B}}(x, y) = \frac{2}{\sqrt{c}} \tanh^{-1}(\sqrt{c} \|-x \oplus y\|)$$



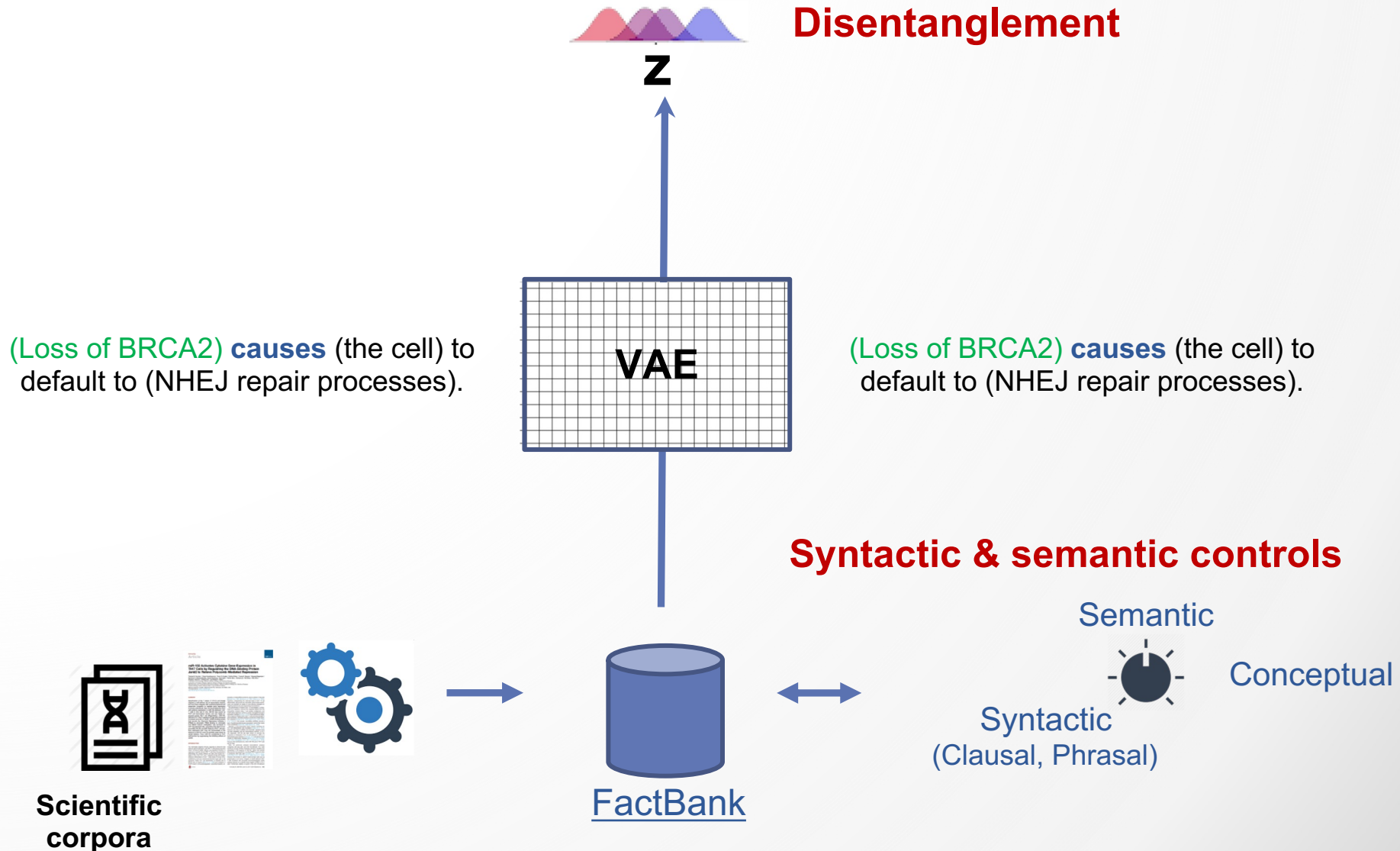


Model	SV-d	MEN-d	SV-t	MEN-t	SL999	SCWS	353	RG	MT
<b>Transformers</b>									
SBERT (bert-base)	13.5	27.8	13.3	30.6	15.1	37.8	20.0	68.1	22.3
SBERT (bert-large)	16.1	23.4	14.4	26.8	13.4	35.7	19.8	60.7	19.1
SBERT (distilroberta)	35.8	61.2	36.7	62.2	43.4	57.1	52.0	77.4	46.2
SBERT (mpnet-base)	45.9	<b>64.9</b>	42.5	<b>67.5</b>	49.5	58.6	56.5	81.3	45.3
SBERT (t5-large)	<b>49.4</b>	63.1	<b>50.2</b>	66.3	<b>57.3</b>	56.1	51.8	<b>85.3</b>	38.1
<b>Multi-Relational</b>									
Euclidean ( $d = 40$ )	39.1	62.9	35.7	65.4	36.3	58.2	52.1	80.9	45.0
Euclidean ( $d = 80$ )	44.1	65.6	39.5	66.2	41.2	58.4	55.8	78.0	42.4
Euclidean ( $d = 200$ )	47.3	67.0	41.0	67.6	43.4	60.6	55.4	78.1	44.6
Euclidean ( $d = 300$ )	47.9	68.3	43.1	69.1	<b>44.7</b>	61.0	54.4	79.0	46.0
Hyperbolic ( $d = 40$ )	36.7	66.2	34.3	66.4	31.8	58.5	50.6	75.5	52.7
Hyperbolic ( $d = 80$ )	42.7	68.2	40.7	68.6	38.3	61.4	59.2	81.0	<b>59.1</b>
Hyperbolic ( $d = 200$ )	48.8	71.8	44.7	73.2	40.7	63.5	64.9	<b>81.6</b>	57.6
Hyperbolic ( $d = 300$ )	<b>50.6</b>	<b>72.6</b>	<b>45.4</b>	<b>74.2</b>	42.3	<b>63.9</b>	<b>66.3</b>	80.5	56.1

T5-large: "Colossal Clean Crawled Corpus" (C4): ~750GB.

MR-Hyperbolic: "CPAE Dictionary": ~19MB.

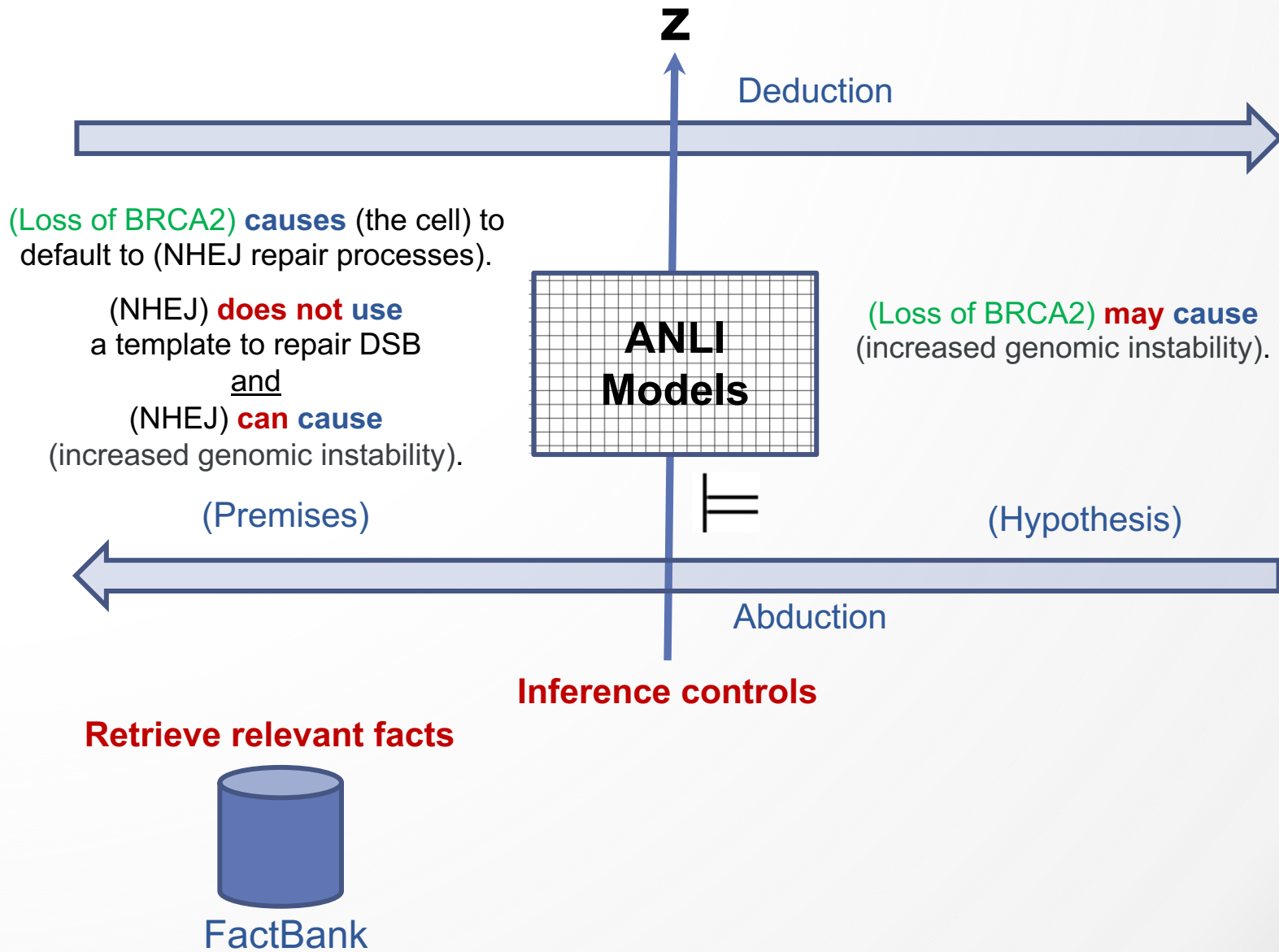
# Sentence-level representation





**Encoding step-wise (multi-hop) inference**

# Encoding Abductive (Explanatory) Reasoning



h: Shale is a sedimentary rock that can be metamorphosed into slate by increased pressure.

'shale is a kind of sedimentary rock'

'high is similar to increase'

'extreme means very high in value'

'slate is a type of metamorphic rock'

'exposure to extreme heat and pressure changes sedimentary and igneous rock into metamorphic rock'

**Abstraction, grounding**

**Abstraction**

Concrete facts tend to share key concepts with the hypotheses and can therefore be effectively retrieved by lexical relevance.

h: Shale is a sedimentary rock that can be metamorphosed into slate by increased pressure.

'shale is a kind of sedimentary rock'

'high is similar to increase'

'extreme means very high in value'

'slate is a type of metamorphic rock'

'exposure to extreme heat and pressure changes sedimentary and  
igneous rock into metamorphic rock'

**Unification**

**Abstraction**

More universal scientific statements tend to be abstract and therefore difficult to rank by means of shared concepts.



h: Shale is a sedimentary rock that can be metamorphosed into slate by increased pressure.

'shale is a kind of sedimentary rock'

'high is similar to increase'

'extreme means very high in value'

'slate is a type of metamorphic rock'

'exposure to extreme heat and pressure changes sedimentary and igneous rock into metamorphic rock'



**Abstraction**

Proposes the composition of two scoring functions:

- A **Relevance Score (RS)** that represents the lexical relevance of a given fact.
- A **Unification Score (US)** that models the explanatory power of a fact according to its frequency in explanations for similar questions

Question(Q):

What is an example of **force** producing heat?

Candidate Answer (C<sub>1</sub>):

Two **sticks** getting warm when **rubbed** **together**

Hypothesis (H<sub>1</sub>):

Two **sticks** getting warm when **rubbed** **together**  
is an example of **force** producing heat

Grounding Facts:

- [✓] a **stick** is an **object**: F<sub>G1</sub>
- [✓] **friction** is a **force**: F<sub>G2</sub>
- [✗] a **pull** is a **force**: F<sub>G3</sub>
- [✓] to **rub** **together** means to **move against**: F<sub>G4</sub>
- [✗] **rubbing** against something is kind of movement: F<sub>G5</sub>

Abstract Facts:

- [✓] **friction** occurs when two **object's** surfaces **move against** each other: F<sub>C1</sub>
- [✓] **friction** causes the temperature of an object to **increases**: F<sub>C2</sub>
- [✗] **magnetic attraction** **pulls** two objects **together**: F<sub>C3</sub>

[✓]: Explanatory Facts

[✗]: Non-Explanatory Facts

### Question(Q):

What is an example of **force** producing heat?

### Candidate Answer (C<sub>1</sub>):

Two **sticks** getting warm when **rubbed** **together**

### Hypothesis (H<sub>1</sub>):

Two **sticks** getting warm when **rubbed** **together** is an example of **force** producing heat

### Grounding Facts:

- [✓] a **stick** is an **object**: F<sub>G1</sub>
- [✓] **friction** is a **force**: F<sub>G2</sub>
- [✗] a **pull** is a **force**: F<sub>G3</sub>
- [✓] to **rub** **together** means to **move against**: F<sub>G4</sub>
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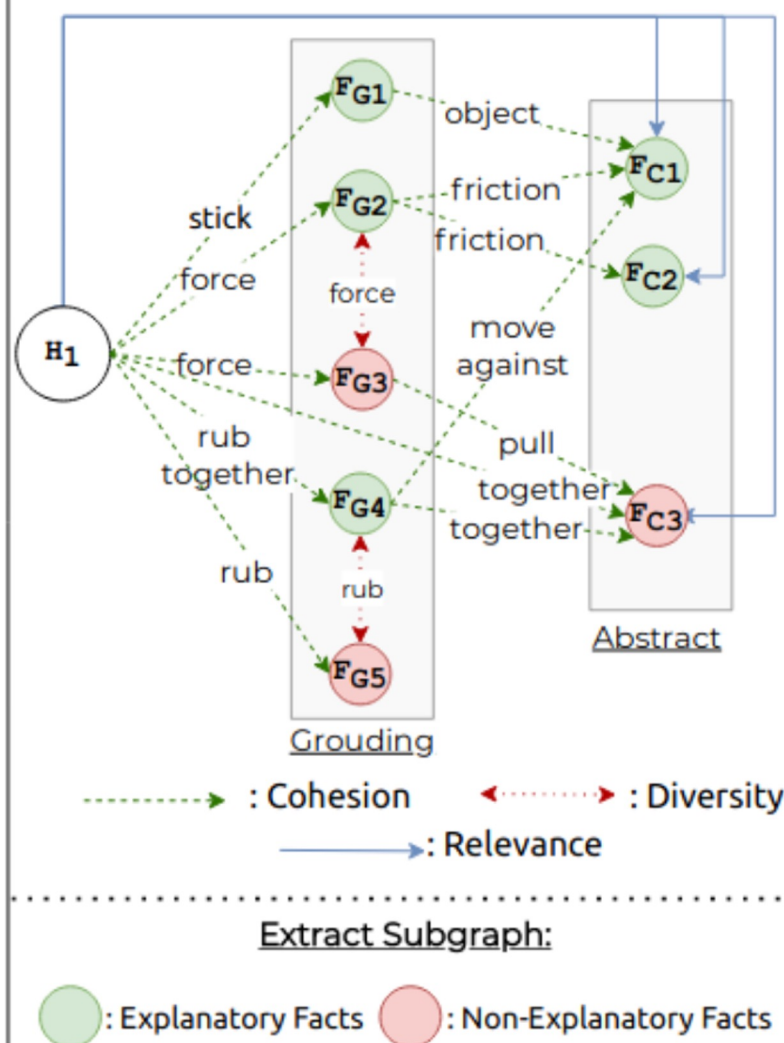
### Abstract Facts:

- [✓] **friction** occurs when two **object's** surfaces **move against** each other: F<sub>C1</sub>
- [✓] **friction** causes the temperature of an object to **increases**: F<sub>C2</sub>
- [✗] **magnetic attraction** **pulls** two objects **together**: F<sub>C3</sub>

[✓]: Explanatory Facts  
[✗]: Non-Explanatory Facts

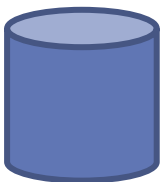
### For each Candidate Hypothesis:

#### Fact Graph Construction:

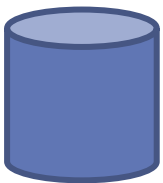


#### Extract Subgraph:

Green circle: Explanatory Facts    Red circle: Non-Explanatory Facts



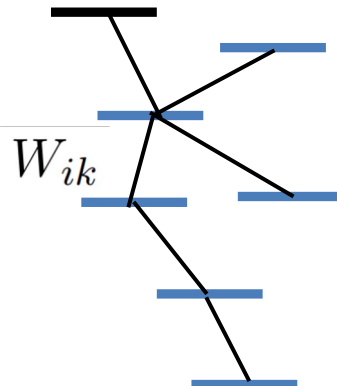
Abstract  
Facts



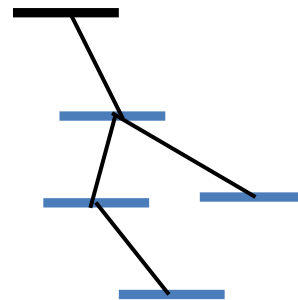
Grounding  
Facts



$\{f_1, f_2, f_3, \dots, f_k\}$



$G = (H, F, E, W)$



Retrieve  
relevant facts

Construct  
a weighted fact graph

Extract subgraph  
via ILP optimization

**Relevance**

**Diversity**

$$D(f_j^{h_i}, f_k^{h_i}) = -1 \frac{|t_{h_i}(f_j^{h_i}) \cap t_{h_i}(f_k^{h_i})|}{\max(|t_{h_i}(f_j^{h_i})|, |t_{h_i}(f_k^{h_i})|)}$$

**Saturation**

$$C(f_j^{h_i}, f_k^{h_i}) = \frac{|t(f_j^{h_i}) \cap t(f_k^{h_i})|}{\max(|t(f_j^{h_i})|, |t(f_k^{h_i})|)}$$

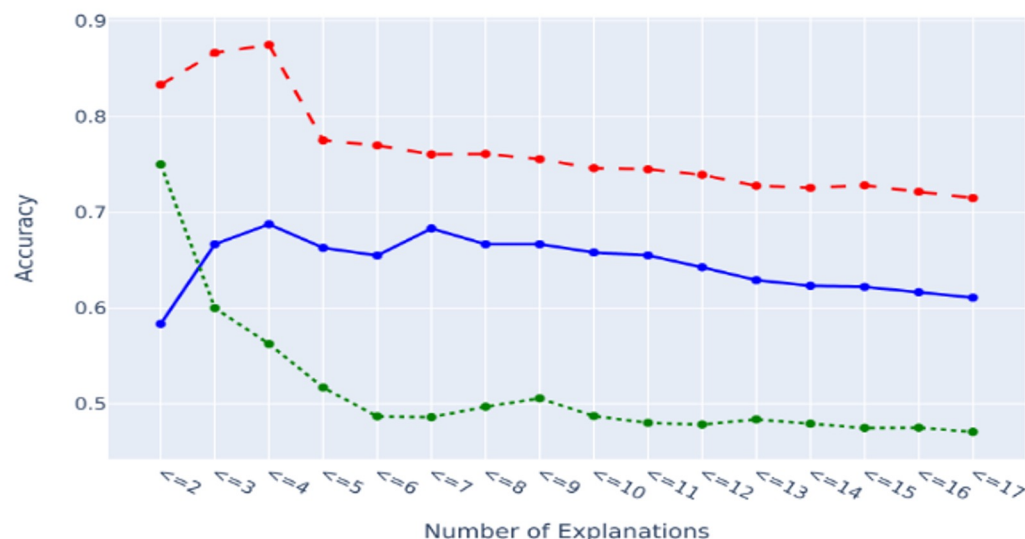
**Prior semantic/inference knowledge**

$$\omega_e(v_j, v_k; \theta_1) = \begin{cases} \theta_{gg} D(v_j, v_k) & v_j, v_k \in F_G^{h_i} \\ \theta_{aa} D(v_j, v_k) & v_j, v_k \in F_A^{h_i} \\ \theta_{ga} C(v_j, v_k) & v_j \in F_G^{h_i}, v_k \in F_A^{h_i} \\ \theta_{qg} C(v_j, v_k) & v_j \in F_G^{h_i}, v_k = h_i \\ \theta_{qa} C(v_j, v_k) & v_j \in F_A^{h_i}, v_k = h_i \end{cases}$$

$$\omega_v(v_i^{h_i}; \theta_2) = \begin{cases} \theta_{lr} L(v_j, h_i) + \theta_{ss} S(v_j, h_i) & v_j \in F_A^{h_i} \\ 0 & v_i \in F_G^{h_i} \\ 0 & v_i = h_i \end{cases}$$



# Approach	Accuracy WT ARC
1 ExplanationLP (Best)	61.37 40.21
<b>Structure</b>	
2 Grounding-Abstract Categories	58.33 35.11
3 Edge weights	43.78 29.45
4 Node weights	42.80 27.81
<b>Cohesion</b>	
5 Hypothesis-Abstract cohesion	38.71 30.31
6 Hypothesis-Grounding cohesion	59.33 38.71
7 Grounding-Abstract cohesion	59.12 38.14
<b>Diversity</b>	
8 Abstract-Abstract diversity	60.16 37.61
9 Grounding-Grounding diversity	60.44 37.71
<b>Relevance</b>	
10 Hypothesis-Abstract semantic similarity	55.38 35.49
11 Hypothesis-Abstract lexical relevance	54.68 36.01



red: ExplanationLP

blue: BERT<sub>Large</sub>

green: PathNet

# of parameters:

- BERTBase: 110M parameters
- BERTLarge: 340M parameters
- ExplanationLP: 9 parameters

# Diff-Explainer: End-to-end abductive learning

An end-to-end differentiable framework that incorporates constraints via convex optimization layers into broader transformers-based architectures.

**Differentiable convex optimization (DCX) layers** (Agrawal et al., 2019) provide a way to encode constraints as part of a deep neural network.

**Problem:** ILP formulation is non-convex and cannot be incorporated into a differentiable convex optimization layer.

## **Solution:**

- Approximate ILP with convex optimization constraints.
- Semi-Definite programming (SDP) is non-linear but convex and has shown to efficiently approximate combinatorial problems.

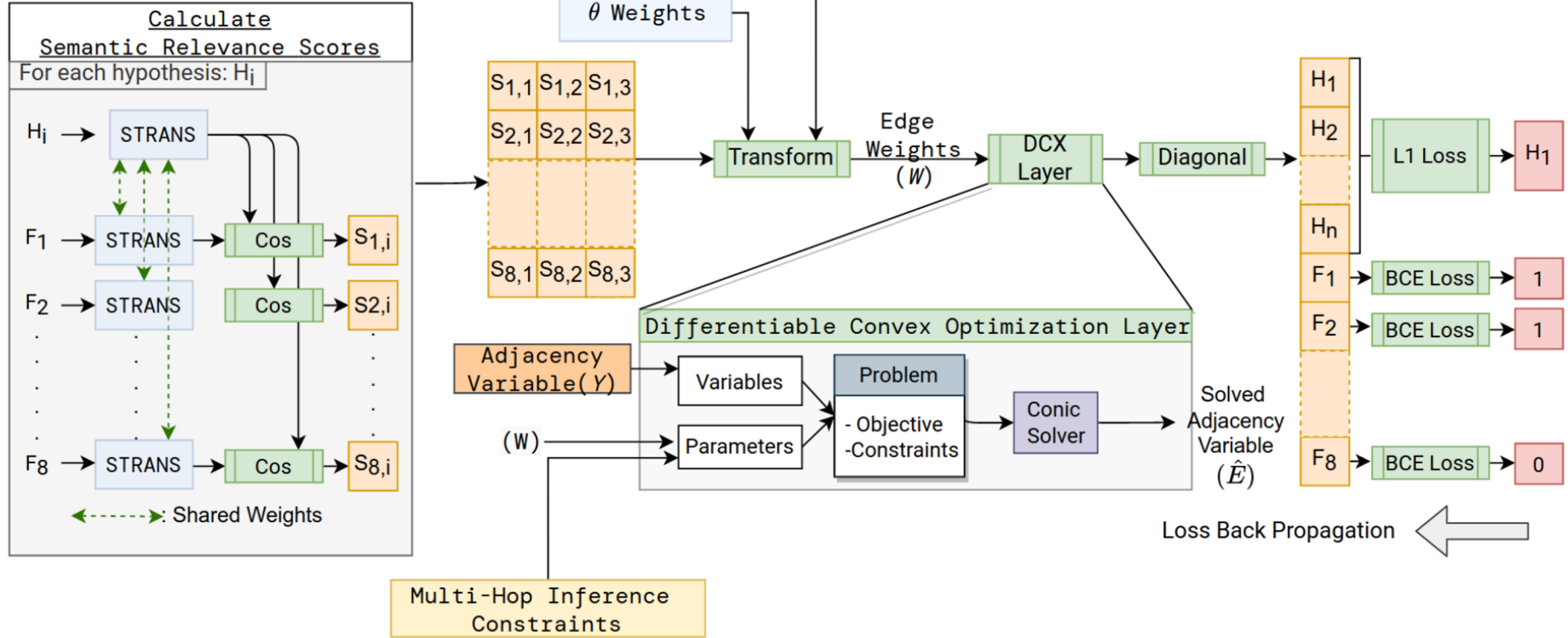
Specifically, we incorporate a differentiable convex optimization layer with Sentence-Transformers (STrans).

# Programmable abductive NLI Solver

## Relevance

$$s_{ij} = S(\vec{h}_i, \vec{f}_j) = \frac{\vec{h}_i \cdot \vec{f}_j}{\|\vec{h}_i\| \|\vec{f}_j\|}$$

## Sentence embeddings



## Saturation

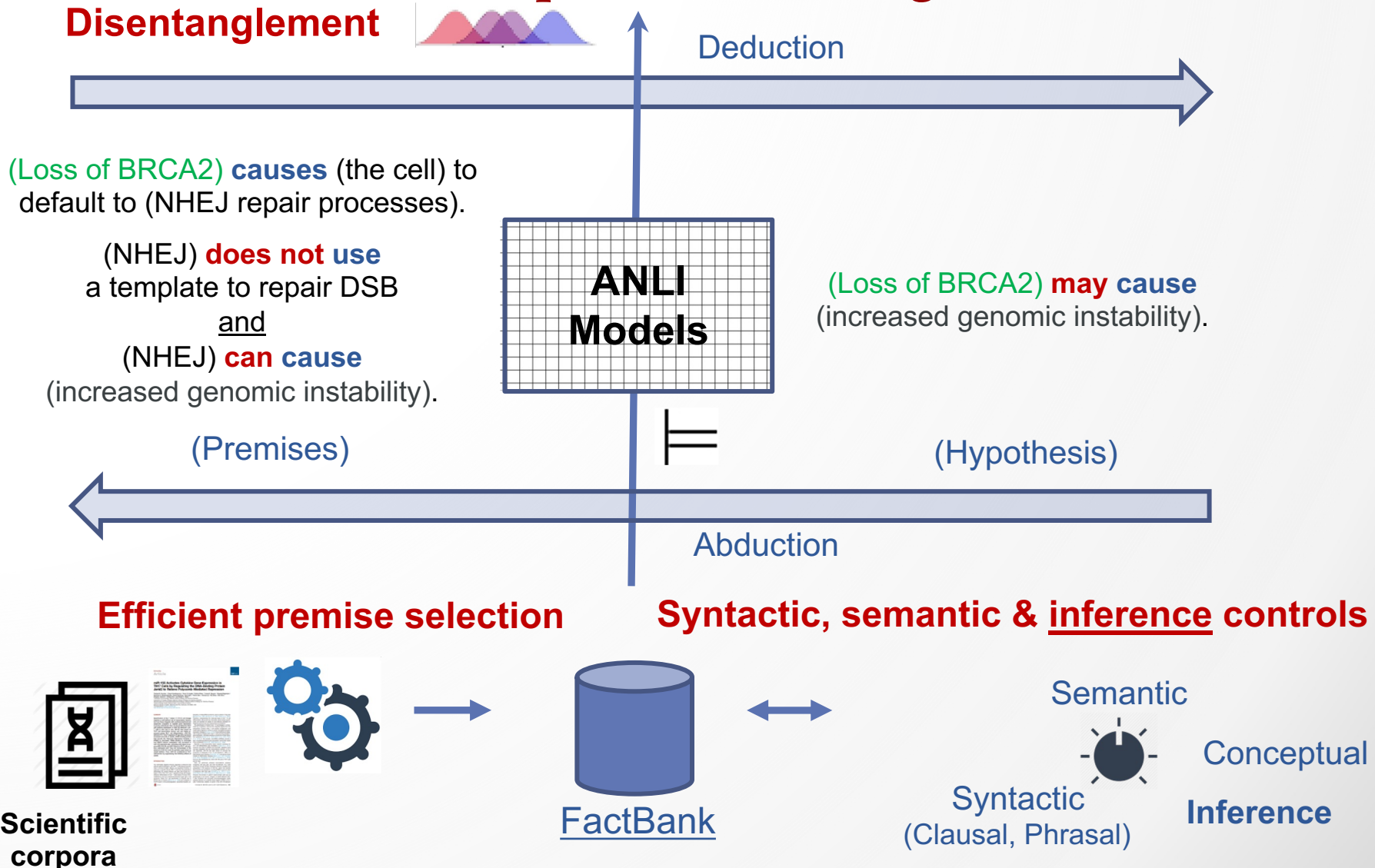
$$l_{ij} = L(h_i, f_j) = \frac{|trm(h_i) \cap trm(f_j)|}{\max(|trm(h_i)|, |trm(f_j)|)}$$

$$W_{ij} = [\theta_1^s, \theta_2^s, \dots, \theta_n^s] \cdot [s_{ij}^{D_1}, s_{ij}^{D_2}, \dots, s_{ij}^{D_n}] + [\theta_1^l, \theta_2^l, \dots, \theta_n^l] \cdot [l_{ij}^{D_1}, l_{ij}^{D_2}, \dots, l_{ij}^{D_n}]$$

## Prior semantic/inference knowledge

# Exploiting the structure of scientific explanations for

## multi-hop inference design





# Encoding abstract, mathematical inference

Conjecture	Premise
Let $T = (S, \tau)$ be a topological space. Let $A, B$ be subsets of $S$ . Then: $\partial(A \cap B) \subseteq \partial A \cup \partial B$ where $\partial A$ denotes the boundary of $A$ .	Let $S, T_1, T_2$ be sets such that $T_1, T_2$ are both subsets of $S$ . Then, using the notation of the relative complement: $ST_1 \cap T_2 = ST_1 \cup ST_2$
$\int \frac{x}{x(x^2-a^2)} = \frac{1}{2a^2}, \ln \frac{x^2-a^2}{x^2} + C$ for $x^2 > a^2$ .	$\int \frac{dx}{x} = \ln x + C$ for $x \neq 0$ .
Let $T = S, \tau$ be a compact space. Then $T$ is countably compact.	Let $T = (S, \tau_{a,b})$ be a modified Fort space. Then $T$ is not a $T_3$ space, $T_4$ space or $T_5$ space.

*STAR: Cross-modal STatement Representation for selecting relevant mathematical premises*

Ferreira & Freitas, EACL (2021)

*To be or not to be an Integer? Encoding Variables for Mathematical Text*

Ferreira et al., EACL (2021)

*Similarity-based equational inference in physics*

Meadows & Freitas, PRR (2021)

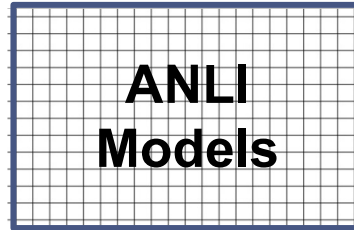
*Premise Selection in Natural Language Mathematical Texts*

Ferreira & Freitas, ACL (2020)

[Abstract statement representation](#)

[Multi-hop mathematical inference](#)

# Interventional, causal and granular evaluation of semantic and inference properties



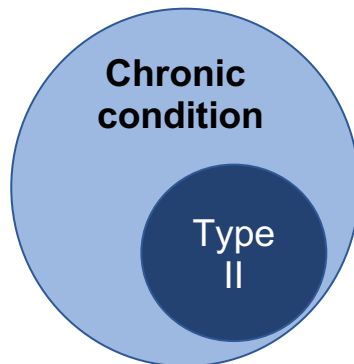
Is reasoning really happening? (**quantifying causal effect**)

Are the semantic features present in the representations? (**probing**)

Do models reveal behavioural consistency? (**metamorphic testing**)

Inferences should follow **logical regularities** based on **abstract semantic features**.

"The patient does not have a **chronic condition**"  $\models$  "The patient does not have **type II Diabetes**"



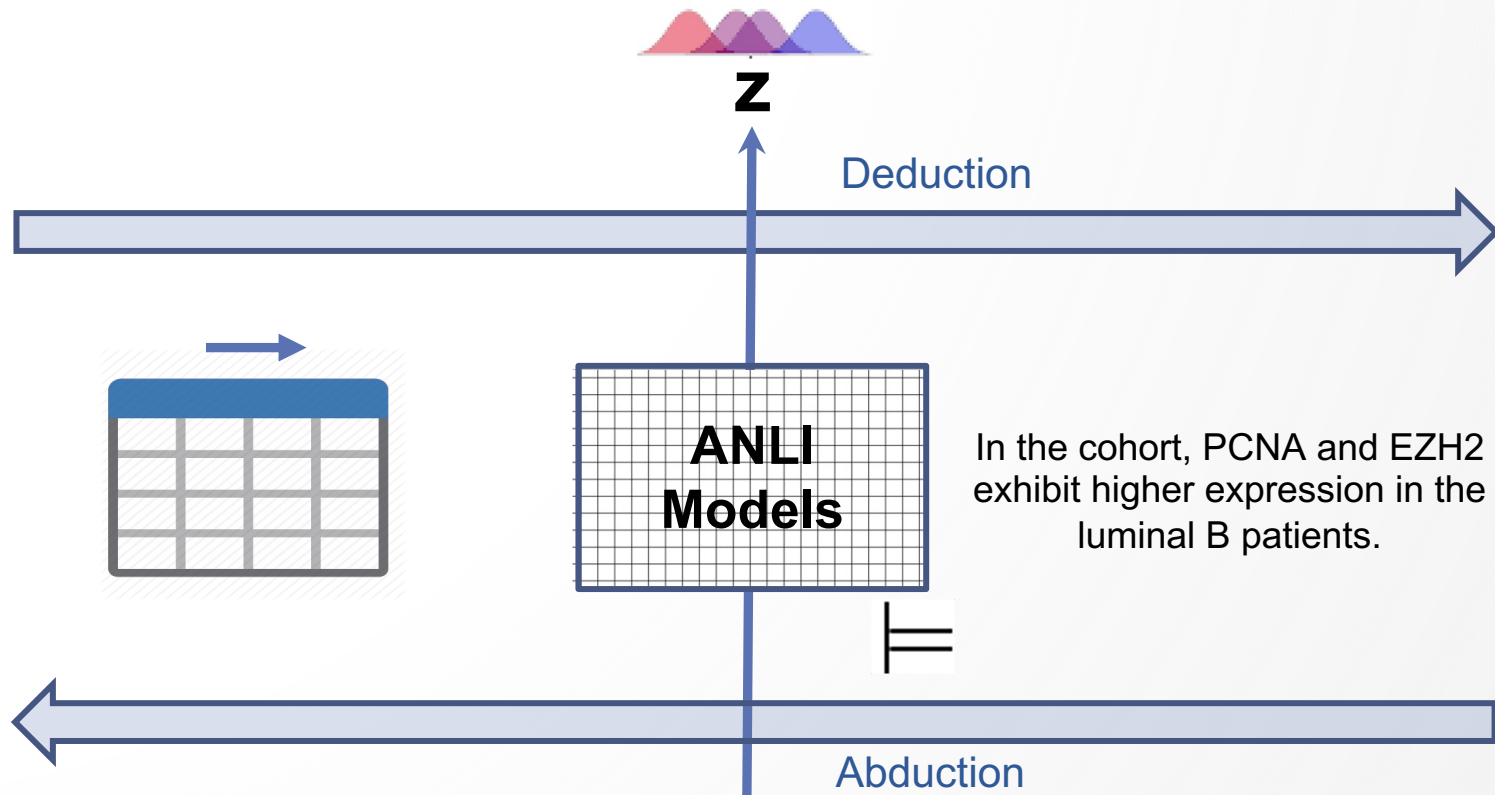
conceptual relations  $\subseteq$  monotonicity

Manino et al. ACL Findings (2022)

Rozanova et al. BlackBoxNLP@EMNLP (2022)

Rozanova et al., NALOMA (2021)

# Encoding inferences over table evidence



# Take away

Building natural language explanation machines for science  
(key neuro-symbolic strategies)

- Granular, controlled, neuro-symbolic inference.
- Integrating and controlling LLMs properties.
- **Sentence-level encoding strategies:**
  - Exploit disentanglement with semantic priors.
  - Use robust lightweight semantic representations.
  - Organise your semantic space.
  - Use specialised strategies for concepts and abstract statements.
- **Inference-level encoding strategies:**
  - Exploit the structure of scientific explanations.
  - Integrate inference priors as constraints.
  - Use differentiable convex layers for end-to-end training.
- **Evaluation of true inference properties:**
  - Determine true reasoning performance by using causal, interventional methods.
  - Probe your model for key properties.
  - Apply systematic behavioural testing.



# Thank you







The northern hemisphere **is a kind** of hemisphere of earth



Abstraction (hemisphere)

a hemisphere of earth **is a kind** of place



Abstraction (place)

If a place **is in** summer, then it **will have** the most sunlight



Unification

Northern hemisphere **will have** the most sunlight in summer

evaporating and condensing can be caused by changes in heat energy

```
graph TD; A[evaporating and condensing can be caused by changes in heat energy] --> B[temperature is a measure of heat energy]; A --> C[evaporating and condensing can be caused by temperature changes]; C --> D[temperature changes can cause phase changes]; C --> E[evaporating and condensing are both phase changes]; E --> F[evaporating is a kind of phase change]; E --> G[condensing is a kind of phase change];
```

temperature is a measure of heat energy

evaporating and condensing can be caused by temperature changes

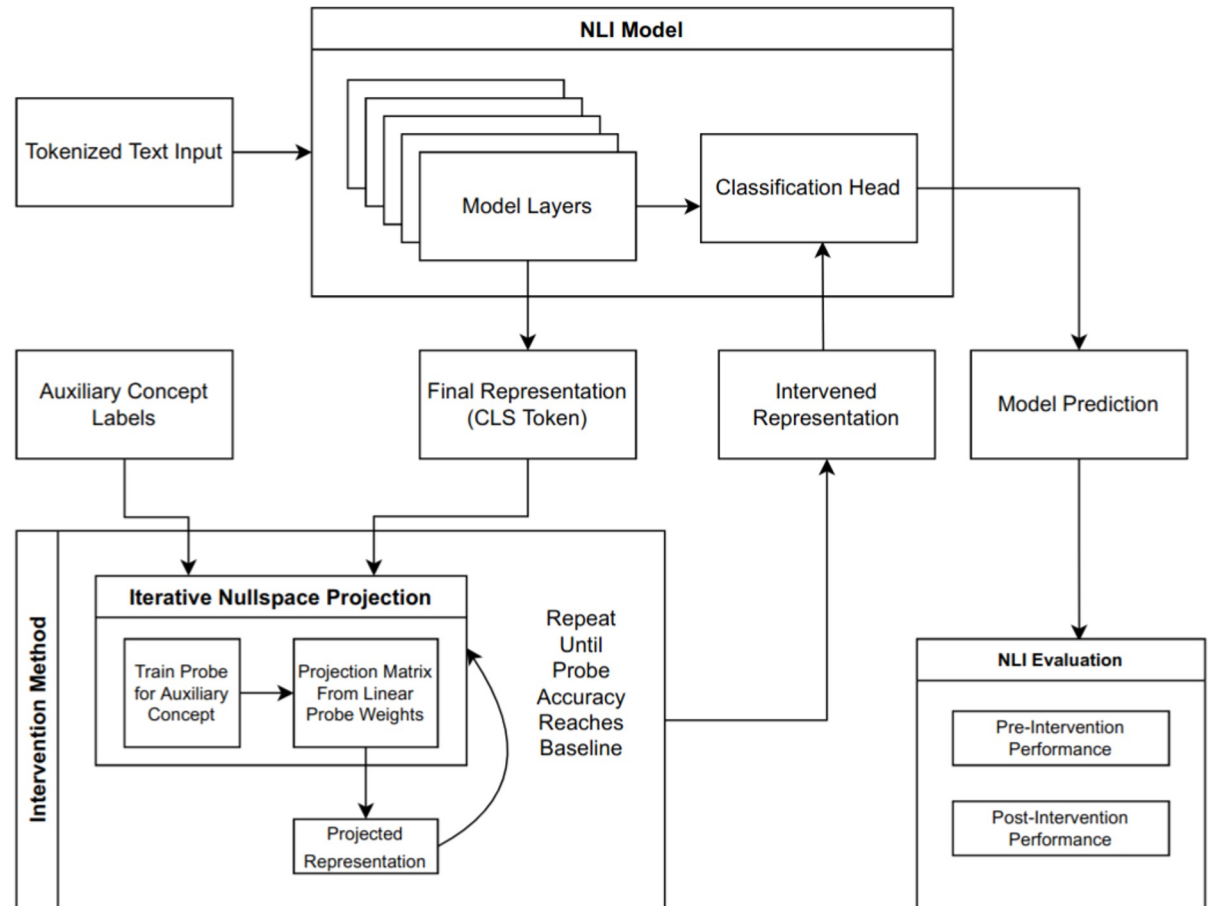
temperature changes can cause phase changes

evaporating and condensing are both phase changes

evaporating is a kind of phase change

condensing is a kind of phase change

# Granular evaluation



Ferreira et al., ACL Demo (2021)

*Does My Representation Capture X?*  
*Probe-Ably*

**Question:** A group of students are studying bean plants. All of the following traits are affected by changes in the environment except . . .

**Candidate answers:** [A] leaf color [B] seed type [C] bean production [D] plant height

---

**Explanation**

- (i) The type of seed of a plant is an inherited characteristic;
- (ii) Inherited characteristics are the opposite of acquired characteristics;
- (iii) An organism's environment affects that organism's acquired characteristics;
- (iv) A plant is a kind of organism;
- (v) A bean plant is a kind of plant;
- (vi) Trait is synonymous with characteristic.



(i) The type of seed of a plant is an inherited characteristic;

$$\forall xy(\text{plant}(x) \wedge \text{seedType}(y, x) \rightarrow \text{characteristic}(y, x) \wedge \text{inherited}(y))$$

(ii) Inherited characteristics are the opposite of acquired characteristics;

$$\forall xy(\text{characteristic}(x, y) \wedge \text{inherited}(x) \rightarrow \neg \text{acquired}(x))$$

(iii) An organism's environment affects that organism's acquired characteristics;

$$\forall xyw(\text{organism}(x) \wedge \text{environment}(y, x) \wedge \text{characteristic}(w, x) \wedge \text{acquired}(w) \rightarrow \\ \rightarrow \exists e(\text{affect}(e) \wedge \text{agent}(e, y) \wedge \text{patient}(e, w)))$$

(iv) A plant is a kind of organism;

$$\forall x(\text{plant}(x) \rightarrow \text{organism}(x))$$

(v) A bean plant is a kind of plant;

$$\forall x(\text{beanPlant}(x) \rightarrow \text{plant}(x))$$

(vi) Trait is synonymous with characteristic.

$$\forall xy(\text{trait}(x, y) \leftrightarrow \text{characteristic}(x, y))$$

$$\forall xy(\text{plant}(x) \wedge \text{seedType}(y, x) \rightarrow \text{characteristic}(y, x) \wedge \text{inherited}(y))$$
$$\forall xy(\text{characteristic}(x, y) \wedge \text{inherited}(x) \rightarrow \neg \text{acquired}(x))$$
$$\forall xyw(\text{organism}(x) \wedge \text{environment}(y, x) \wedge \text{characteristic}(w, x) \wedge \text{acquired}(w) \rightarrow$$

**KB**  $\Phi$   $\rightarrow \exists e(\text{affect}(e) \wedge \text{agent}(e, y) \wedge \text{patient}(e, w))$

$$\forall x(\text{plant}(x) \rightarrow \text{organism}(x))$$
$$\forall x(\text{beanPlant}(x) \rightarrow \text{plant}(x))$$
$$\forall xy(\text{trait}(x, y) \leftrightarrow \text{characteristic}(x, y))$$

---

$$\Phi \models \psi ?$$

**Question:** find a characteristic of plants not affected by those plants' environments.  
That is, we are asked for a **P** making the schematic formula **true**.

$$\psi$$
$$\forall xyzwe(\text{beanPlant}(x) \wedge \text{environment}(y, x) \wedge \text{changeIn}(z, y) \wedge \text{trait}(w, x) \wedge \text{affect}(e) \wedge \text{agent}(e, z) \wedge \mathbf{P} \rightarrow \neg \text{patient}(e, w))$$

**P:**  $\text{seedType}(w, x)$

**Question:** How a 1 degree rise in temperature will affect the grape harvest in Valais?

Evidence-based  
explanation

Optimal Wine Grape Temperatures Over the Growing Season		
Variety	Min	Max
Pinot Gris	13°C	15°C
Riesling	13°C	17°C
Pinot Noir	14°C	15°C
Chardonnay	14°C	18°C
Sauvignon Blanc	14°C	18°C
Syrah	16°C	19°C
Table Grapes	19°C	22°C

Fine wine production is likely to shift due to climate change. Among agricultural products, wine grapes are one of the most sensitive crops to variations in temperature and precipitation

Since the year 1864, the temperature in the Canton of Valais has increased by 2 °C. If global greenhouse gas emissions continue to rise in the future, the warming will continue and will amount to further 3 °C by 2060 with respect to the mean of the period 1981-2010.

Pinot Noir accounts for 11% of the grape production in Valais.

Availability by Grape/Blend =-Valais	
Pinot Noir	11%
Petite Arvine	9%
Chasselas	9%
Syrah	8%
Rare Red Blend	7%
Corlanin	6%
Gamay Pinot Noir	6%
Other	43%

Temperature Deviation - Valais (°C)		RCP2.6			RCP8.5		
		min	mid	max	min	mid	max
Summer	2035	0.8	1.8	2.5	1.7	2.0	3.0
	2060	1.0	1.9	3.1	2.7	3.9	5.7
Winter	2035	0.6	1.0	1.8	0.9	1.7	1.9
	2060	0.8	1.5	1.9	1.8	2.2	2.9

Precipitation Deviation - Valais (%)		RCP2.6			RCP8.5		
		min	mid	max	min	mid	max
Summer	2035	-18	-1	5	-10	-3	4
	2060	-15	0	12	-20	-12	12
Winter	2035	-10	8	20	2	15	22
	2060	-3	12	20	0	12	22

# **Claim:** US Summer Youth Employment programs can be replicated in Central Europe to help low income youth overcome barriers to accessing jobs.

## Labor

SYEPs disproportionately serve youth from low-income households that typically face higher than average barriers to entering the labor market

	New York City 2006 – 2010	Boston 2015	Chicago 2012
Youth offered SYEP job	72.3%	83.6%	78.7%
Youth not offered SYEP job	18.5%	26.4%	15.2%

The move toward evidence-based policy (EBP) formation still requires improvement of the understanding of the role of evidence within policy process and analysis of the barriers in using evidence in policy development processes

For the most part, SYEPs do not increase rates of formal sector employment for the average participant after the program ends, with some exceptions

SYEP participation decreases arrests and convictions during the program summer

## Criminal Justice System

SYEPs consistently reduce involvement in the criminal justice system for participating youth for the duration of the program and at least a year beyond.

Youth at greater risk of experiencing socially costly outcomes, such as involvement with the criminal justice system or disengagement from school, are shown to experience the greatest benefits from SYEP.

	Control	Participants	Impact
Violent crime arrests per hundred youth	18.34%	11.96%	-6.38%

## Education

Evidence on SYEPs' role in improving educational outcomes is mixed.

On average, in the studies that showed positive effects in academic outcomes, those who benefited were youth of legal drop-out age and youth who had a higher rate of school absences prior to program participation.

Outcomes suggests improvements in social-emotional skills, academic and career aspirations, and work habits associated with job readiness.

**Claim:** it is not necessary to prove the absence of the debtor's assets to obtain the disregard of legal personality.

**Precedent N° 1.729.554 (Superior Court):** “In fact, the disregard of the legal personality can be decreed even if insolvency is not configured, provided that the deviation of purpose or the patrimonial confusion, characterizing the abuse of personality, are verified.”

**Law 13105 (Federal - CPC): Art. 134:** The incident of disregard is applicable at all stages of the acknowledgement process, in the execution of the sentence and in the execution based on an extrajudicial enforcement order

**Law 13105 (Federal - CPC) Art. 134 § 4:** The application must demonstrate the completion of the specific legal presuppositions for disregarding the legal personality.

**Law 10406/02 (Federal – Civil code) Art. 50:** In case of abuse of legal personality, characterized by the misuse of purpose, or by the confusion of assets, the judge may decide, at the request of the party, or of the Public Prosecutor's Office when it is up to him to intervene in the process, that the effects of certain and certain relationships of obligations are extended to the private assets of the administrators or partners of the legal entity.

**Doctrine (Humberto Dalla):** “In the case of greater disregard, in which the true passive holder of the credit is the partner (who acted abusively through the legal entity), the author has the right to choose his liability, regardless of the potential satisfaction of the credit before the legal entity.”



# Complex Sentence Representation

- Clausal-Phrasal Disembedding (CPD).
- Minimal, localised, self-contained propositions.

“Programmed death-ligand 1 (PD-L1) also known as cluster of differentiation 274 (CD274) or B7 homolog 1 (B7-H1) is a protein that in humans is encoded by the CD274 gene.”

Core: PD-L1 is encoded by the CD274 gene.

Context: This is in humans.

PD-L1 is also known as cluster of differentiation 274.

PD-L1 is also known as B7-H1.

PD-L1 is a protein.

Programmed death-ligand 1 has abbreviation PD-L1.

Cluster of differentiation 274 has abbreviation CD274.

B7 homolog 1 has abbreviation B7-H1.

# Complex Sentence Representation

“Programmed death-ligand 1 (PD-L1) also known as cluster of differentiation 274 (CD274) or B7 homolog 1 (B7-H1) is a protein that in humans is encoded by the CD274 gene.”

Core: **is encoded by**(e, PD-L1, the CD274 gene).

Context: **in**(e, humans).

**is also known as**(PD-L1, cluster of differentiation 274).

**is also known as**(PD-L1, B7-H1).

**is a**(PD-L1, protein).

**has abbreviation**(Programmed death-ligand 1, PD-L1).

**has abbreviation**(Cluster of differentiation 274, CD274).

**has abbreviation**(B7 homolog 1, B7-H1).

# Complex Sentence Representation

	CLAUSAL/PHRASAL TYPE	HIERARCHY	# RULES
<b>Clausal disembedding</b>			
1	Coordinate clauses	coordinate	1
2	Adverbial clauses	subordinate	6
3a	Relative clauses (non-restrictive)	subordinate	5
3b	Relative clauses (restrictive)	subordinate	4
4	Reported speech	subordinate	4
<b>Phrasal disembedding</b>			
5	Coordinate verb phrases	coordinate	1
6	Coordinate noun phrases	coordinate	2
6	Participial phrases	subordinate	4
8a	Appositions (non-restrictive)	subordinate	1
8b	Appositions (restrictive)	subordinate	1
9	Prepositional phrases	subordinate	3
10	Adjectival and adverbial phrases	subordinate	2
11	Lead NPs	subordinate	1
	Total		35

System	Precision	Recall	F <sub>1</sub>	AUC
REVERB	-7.2%	+19.1%	+8.4%	<b>+39.2%</b>
OLLIE	+1.1%	-1.5%	-0.3%	-1.1%
ClausIE	+17.0%	-3.5%	+8.1%	+13.0%
Stanford	<b>+25.0%</b>	<b>+27.2%</b>	<b>+25.5%</b>	+35.5%
Open IE				
PropS	-6.1%	+16.9%	+4.5%	+12.4%
OpenIE-4	+10.0%	+8.6%	+9.4%	+19.6%
MinIE	+23.7%	-1.8%	+12.5%	+21.3%
OpenIE-5	+5.0%	+4.2%	+4.6%	+9.0%
RnnOIE	-15.0%	+0.9%	-8.3%	-14.1%